Semi-Supervised Image Dehazing
Lerenhan Li, Yunlong Dong, Wenqi Ren, Jinshan Pan, Changxin Gao, Nong Sang, and Ming-Hsuan Yang, Fellow, IEEE

Abstract—We present an effective semi-supervised learning algorithm for single image dehazing. The proposed algorithm applies a deep Convolutional Neural Network (CNN) containing a supervised learning branch and an unsupervised learning branch. In the supervised branch, the deep neural network is constrained by the supervised loss functions, which are mean squared, perceptual, and adversarial losses. In the unsupervised branch, we exploit the properties of clean images via sparsity of dark channel and gradient priors to constrain the network. We train the proposed network on both the synthetic data and real-world images in an end-to-end manner. Our analysis shows that the proposed semi-supervised learning algorithm is not limited to synthetic training datasets and can be generalized well to real-world images. Extensive experimental results demonstrate that the proposed algorithm performs favorably against the state-of-the-art single image dehazing algorithms on both benchmark datasets and real-world images.

Index Terms—Image dehazing, deep learning, semi-supervised learning.

I. INTRODUCTION

INGLE image dehazing aims to recover the clean image from a hazy one. It has been an active research effort in the vision and graphics community due to the challenges in problem formulation, regularization, and optimization. Mathematically, the hazing process [7] can be formulated as

\[ I(x) = J(x)t(x) + A(1 - t(x)), \]

where \( I(x) \), \( J(x) \), \( A \), and \( t(x) \) denote a hazy image, clean image, global atmospheric light, and a transmission map, respectively. When the haze is homogeneous, the transmission map \( t(x) \) can be expressed as \( t(x) = e^{-\beta d(x)} \), where \( d(x) \) is the scene depth and \( \beta \) is the medium extinction coefficient. As only the hazy image \( I(x) \) is available, the problem is ill-posed.

To make the problem well posed, existing algorithms usually make assumptions on the clean images [6], [7], e.g., the dark channel prior [7] and color-line priors [6]. As image priors often involve non-convex and non-linear terms, such approaches entail high computational loads.

To overcome this problem, deep convolutional neural networks (CNNs) have been used for image dehazing [2], [15], [18], [28]–[30], [43]. Typically, deep CNNs are used either to estimate transmission maps [2], [28], [43] or predict clean images directly [15], [18], [29]. These methods are efficient and outperform the hand-crafted prior based algorithms with significant performance gains. However, deep learning based approaches usually require a large number of ground-truth images for training. Most of them are trained on synthetic hazy datasets (e.g., NYU Depth dataset [37] and Make3D dataset [33]–[35]). As these synthetic hazy datasets contain limited image categories and image depths, the performance of existing deep learning based algorithms is usually limited to synthetic training datasets and cannot be well generalized to real-world hazy images.

To this end, we propose a semi-supervised learning network for image dehazing using both synthetic and real-world hazy images. Specifically, we design a deep network consisted of a supervised branch and an unsupervised branch, both of which share the weights during the training process. The supervised branch is trained on synthetic hazy images while the unsupervised one is trained on real hazy images. In the supervised branch, we apply labeled losses such as mean squared loss, perceptual loss, and adversarial loss to train the network with the difference between estimated results and ground-truths.

To avoid the supervised branch over-fitting the training dataset, we exploit the properties of clear images via the dark channel (DC) [7] and image gradients such as total variation (TV) [32] to constrain the unsupervised branch. The whole network is trained on both the synthetic data and real-world images in an end-to-end manner. With the semi-supervised learning approach, our network performs favorably against the state-of-the-art dehazing approaches. Figure 1 shows an example on a real-world hazy image, where the proposed method generates a cleaner image.

Manuscript received March 13, 2019; revised August 7, 2019 and October 2, 2019; accepted October 23, 2019. Date of publication November 15, 2019; date of current version January 23, 2020. This work was supported in part by the National Natural Science Foundation of China under Grant 61430007, Grant 61901184, Grant 61872421, and Grant 61922043, in part by the Natural Science Foundation of Jiangsu Province under Grant BK20180471, and in part by the National Science Foundation CAREER under Grant 1149783. The work of W. Ren was supported in part by the CCF-DiDi GAIA (YF20180101) and in part by the Zhejiang Lab’s International Talent Grant 1149783. The work of L. Li was supported in part by the scholarship from the China Scholarship Council. The associate editor coordinating the review of this manuscript and approving its publication was Dr. Xin Li (Lerenhan Li and Yunlong Dong contributed equally to this work.) (Corresponding author: Nong Sang.)

L. Li, Y. Dong, C. Gao, and N. Sang are with the National Key Laboratory of Science and Technology on Multi-spectral Information Processing, School of Artificial Intelligence and Automation, Huazhong University of Science and Technology, Wuhan 430074, China (e-mail: lhl@hust.edu.cn; dyi@hust.edu.cn; ccgo@hust.edu.cn; nsang@hust.edu.cn).

W. Ren is with the Institute of Information Engineering, Chinese Academy of Sciences, Beijing 100049, China (e-mail: rwq.renwenqi@gmail.com).

J. Pan is with the Intelligent Media Analysis Group, School of Computer Science, Nanjing University of Science and Technology, Nanjing 210094, China (e-mail: sduran@gmail.com).

M.-H. Yang is with the School of Engineering, University of California at Merced, Merced, CA 95534 USA (e-mail: mhyang@ucmerced.edu).

Digital Object Identifier 10.1109/TIP.2019.2952690

Authorized licensed use limited to: Univ of Calif Merced. Downloaded on February 28, 2021 at 22:10:53 UTC from IEEE Xplore. Restrictions apply.
The contributions of this work are as follows:

- We propose a semi-supervised algorithm to learn the relationship between synthetic and real-world hazy images. The proposed network consists of a supervised branch and an unsupervised branch.
- We exploit conventional image priors as unlabeled losses to train the unsupervised branch with real training data.
- We conduct extensive experiments and demonstrate that the proposed semi-supervised dehazing method performs favorably against the state-of-the-art dehazing approaches both on the synthetic datasets as well as real hazy images.

II. RELATED WORK

In this section, we discuss the prior based and learning based single image dehazing algorithms, and semi-supervised learning methods for low-level vision tasks.

A. Prior-Based Single Image Dehazing

Prior based methods focus on exploiting statistical properties of images to estimate transmission maps and atmospheric light. Tan [38] proposes a contrast-maximization image restoration method based on the observations that images with enhanced visibility (or clear-day images) have more contrast than images plagued by bad weather, and air light whose variation mainly depends on the distance of objects to the viewer, tends to be smooth. He et al. [7] develop an image restoration method by enforcing the sparsity on the dark channel of a recovered image based on the observations that the dark channel of the clean image is sparser than that of the hazy image. Several approaches have since been developed to improve efficiency and performance of image restoration based on the dark channel prior [19], [21], [23], [40], [41]. In addition, Zhu et al. [45] estimate the scene depth of the hazy images and remove the haze based on a color attenuation prior. Fattal [6] develops a color-line prior based on the observation that small image patches typically exhibit a 1D distribution in the RGB color space. Similarly, Berman et al. [1] approximate the colors of a clean image by distinct chromatic properties and use them as the prior on haze-free images.

However, prior based image restoration methods usually entail solving non-convex optimization problems with computationally expensive steps. Furthermore, it may not perform well when the assumed priors do not hold for some specific scenes [7].

B. Learning-Based Single Image Dehazing

Numerous deep CNN models have been proposed for low-level vision problems such as super-resolution [9], [12], denoising [20], [27], and image deblurring [17], [36], [39]. A number of methods [2], [28], [43] apply deep CNNs to estimate the transmission maps and atmospheric light first, and then recover the clean image by an element-wise division based on the degradation model in (1). Ren et al. [28] learn the mapping from hazy inputs to transmission maps using a coarse-to-fine strategy. On the other hand, Zhang and Patel [43] propose to estimate transmission maps by a densely connected pyramid network while estimating the atmospheric light via a U-Net [31]. However, these approaches may introduce artifacts and color distortion when the estimated transmission maps and atmospheric light are not accurate. To remedy this, some end-to-end methods [15], [18], [29] do not estimate the transmission map or atmospheric light, and learn to recover the clean image directly. Ren et al. [29] present a gated fusion network by fusing three images derived from the original hazy input (e.g., white balanced, contrast enhanced, and gamma corrected), which may suffer from color distortion due to pre-processing. Li et al. [18] develop a method to restore clean images by training conditional Generative Adversarial Networks (GANs).

The aforementioned learning methods use synthetic images and may not perform well on real images due to the domain gap. On the other hand, a number of algorithms apply unpaired data to train the network based on the physics model [42] or cycle GAN [4]. However, only applying the unlabeled or unpaired data is less effective than using the labeled or paired data to train the network. Different from the existing CNN based approaches, our network is trained on both synthetic and real data in a semi-supervised manner, and adapts to different image domains.

C. Semi-Supervised Learning

A few semi-supervised learning methods [11], [13] have been recently proposed to solve the low-level vision tasks. Kuznietsov et al. [11] train a deep network to predict depth maps by adding the image alignment error and regularization cost to enforce smoothness of the estimated depth maps. Without any prior assumptions in optical flow estimation, Lai et al. [13] propose a discriminator to distinguish the flow warp error between labeled and unlabeled data. In these approaches, the design of reconstruction errors in the unsupervised branches is based on the domain-specific knowledge, which cannot be directly applied to image dehazing.
Fig. 2. Proposed semi-supervised learning framework for single image dehazing. The proposed method consists of two branches sharing the same weights. The supervised branch is trained using labeled synthetic data and loss functions based on mean squared, perceptual, and adversarial errors. The unsupervised branch is trained using unlabeled real data and loss functions based on dark channel loss and total variation.

### TABLE I

<table>
<thead>
<tr>
<th>Layer</th>
<th>Conv1</th>
<th>Res2-4</th>
<th>Conv5</th>
<th>Res6-8</th>
<th>Conv9</th>
<th>Res10-15</th>
<th>Upconv16</th>
<th>Res17-19</th>
<th>Upconv20</th>
<th>Res21-23</th>
<th>Conv24</th>
<th>Tanh</th>
</tr>
</thead>
<tbody>
<tr>
<td>In_channels</td>
<td>3</td>
<td>64</td>
<td>64</td>
<td>128</td>
<td>128</td>
<td>256</td>
<td>256</td>
<td>128</td>
<td>128</td>
<td>64</td>
<td>64</td>
<td>3</td>
</tr>
<tr>
<td>Out_channels</td>
<td>64</td>
<td>64</td>
<td>128</td>
<td>128</td>
<td>256</td>
<td>256</td>
<td>128</td>
<td>128</td>
<td>64</td>
<td>64</td>
<td>3</td>
<td>3</td>
</tr>
<tr>
<td>Kernel size</td>
<td>7</td>
<td>-</td>
<td>5</td>
<td>-</td>
<td>3</td>
<td>-</td>
<td>4</td>
<td>-</td>
<td>4</td>
<td>-</td>
<td>7</td>
<td>-</td>
</tr>
<tr>
<td>Stride</td>
<td>1</td>
<td>-</td>
<td>2</td>
<td>-</td>
<td>2</td>
<td>-</td>
<td>2</td>
<td>-</td>
<td>2</td>
<td>-</td>
<td>1</td>
<td>-</td>
</tr>
<tr>
<td>Pad</td>
<td>3</td>
<td>-</td>
<td>1</td>
<td>-</td>
<td>1</td>
<td>-</td>
<td>1</td>
<td>-</td>
<td>1</td>
<td>-</td>
<td>3</td>
<td>-</td>
</tr>
<tr>
<td>Sum</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>Input</td>
</tr>
</tbody>
</table>

Thus, we propose to train the unsupervised branch with conventional dark channel and total variation loss functions.

### III. PROPOSED ALGORITHM

Existing deep CNN-based image dehazing algorithms are usually developed within the supervised learning framework, which is limited to the specific synthetic training data. In this work, we address this problem with a semi-supervised learning approach. Specifically, we train a deep CNN for image dehazing using a labeled dataset \( \{I_i, J_i\}_{i=1}^{N_l} \) and an unlabeled dataset \( \{I_i\}_{i=1}^{N_u} \), where \( N_l \) and \( N_u \) denote the numbers of the labeled and unlabeled training images, respectively. In addition, \( I_i \) and \( J_i \) denote the \( i \)-th hazy image and the corresponding ground-truth clean image. We train a network to learn haze-free images \( J \) from hazy inputs \( I \):

\[
J = \mathcal{G}(I), \tag{2}
\]

where \( \mathcal{G}(\cdot) \) denotes the proposed network consisting of a supervised branch \( \mathcal{G}_s \) and an unsupervised branch \( \mathcal{G}_u \). Both branches share the same weights during the training. We summarize the proposed network in Figure 2 and present the detailed network architecture in the following section.

#### A. Network Architecture

We use an encoder-decoder architecture with skip connections which has been shown effective for low-level tasks [13], [36], [39]. We show the architecture and configurations of the proposed network in Figure 2 and Table I. The encoder contains three scales and each consists of three stacked residual blocks. Similar to the work by Nah et al. [22], we do not use any normalization layer in the residual blocks. The configurations of the residual blocks are shown in Table II. The numbers of the input and output channels of the residual blocks are the same as those in Table I.

We use the Stride-Conv layer to down-sample the feature maps from the previous scale by 1/2. The decoder contains three scales and each is also stacked by three residual blocks. We use the Transposed-Conv layer to up-sample the features by the factor of 2. Each convolution layer is followed by a non-linear ReLU layer except for Conv24. We skip-connect the feature maps by the summation operation. In addition, we use the residual learning to learn the difference between hazy and clean images. We analyze the effect of each component of the network in Section V-D.

For adversarial learning, we construct a discriminator by a conventional classifier, stacked by a branch of convolution,
non-linear ReLU, and instance normalization layers. The details of the discriminator are shown in Table III.

### B. Training Losses

We use supervised and unsupervised losses to train the corresponding branches.

1) **Supervised Losses:** We use the mean squared loss to ensure the predicted image $\hat{J}$ is close to the ground-truth $\hat{J}$:

$$L_c = \frac{1}{N_j} \sum_{i=1}^{N_j} \left\| \mathbf{J}_i - \hat{\mathbf{J}}_i \right\|_2^2,$$

where $N_j$ denotes the number of labeled data in a mini-batch. In addition, $\mathbf{J}$ and $\hat{\mathbf{J}}$ represent the vector forms of the predicted image $\hat{J}$ and the corresponding ground-truth image $\hat{J}$, respectively. To generate photo-realistic images, we also use the perceptual loss based on the pre-trained VGG-19 network [8]:

$$L_p = \frac{1}{N_j} \sum_{i=1}^{N_j} \left\| \mathbf{F}_{\mathbf{J}_i} - \mathbf{F}_{\hat{\mathbf{J}}_i} \right\|_2^2,$$

where $\mathbf{F}_{\mathbf{J}_i}$ and $\mathbf{F}_{\hat{\mathbf{J}}_i}$ denote the vector forms of the feature maps w.r.t. the predicted image $\hat{J}$ and its corresponding ground-truth $\hat{J}$, respectively. The feature maps are from the conv3–3 layer of the VGG-19 network that is pre-trained on the ImageNet [3].

To generate sharp and visually pleasing images, we follow the GAN model [14] and build a discriminator $D_{\text{ls}}$ to distinguish whether an image is produced by the generator $G$ (i.e., $\hat{J}$) or from the ground-truth of labeled data (i.e., $\hat{J}$). The adversarial loss can be expressed as:

$$L_a = \mathbb{E}_\hat{\mathbf{J}} \left[ \log D_{\text{ls}}(\hat{\mathbf{J}}) \right] + \mathbb{E}_\mathbf{J} \left[ \log(1 - D_{\text{ls}}(\mathbf{J})) \right].$$

2) **Unsupervised Losses:** We use the total variation and dark channel losses to enforce the unsupervised branch to generate images that have the same statistical properties as clean images. The total variation loss, an $\ell_1$-regularization gradient prior on the predicted images by the unsupervised branch, is applied to preserve structures and details:

$$L_t = \frac{1}{N_u} \sum_{i=1}^{N_u} \left( \| \nabla_x \mathbf{J}_i \|_1 + \| \nabla_y \mathbf{J}_i \|_1 \right),$$

where $\nabla_x$ and $\nabla_y$ represent the horizontal and vertical differential operation matrices, respectively.

The dark channel of clean images [7], [24] has been shown to be sparser than that of the hazy ones. It can be expressed by:

$$D(I) = \min_{y \in N(x)} \left[ \min_{c \in [r, g, b]} I^c(y) \right],$$

where $x$ and $y$ are pixel coordinates, $I^c$ denotes $c$-th color channel, and $N(x)$ is an image patch centered at $x$. Motivated by this, we apply an $\ell_1$-regularization to constrain the sparsity of the dark channel of the predicted images:

$$L_d = \frac{1}{N_u} \sum_{i=1}^{N_u} \| \mathbf{D}_{\mathbf{J}_i} \|_1,$$

where $\mathbf{D}_{\mathbf{J}_i}$ denotes the vector form of the dark channel of the predicted image $\mathbf{J}_i$.

Although the dark channel has been shown effective to remove the haze by adding the constraint on the clean image [7], it is challenging to embed into the learning network due to the highly non-convex and non-linear term. We apply the look-up table scheme [24] to implement the forward and backward step of the dark channel operation. Figure 3 shows a toy example on how the operations are carried out using the look-up table scheme.

We apply a matrix of $5 \times 5$ to represent a single channel image. Based on (7), in the forward stage, the dark channel of the image is computed as:

$$D(I) = \min_{y \in N(x)} [I(y)],$$

where the size of the patch $N(y)$ is set as $3 \times 3$. As shown in Figure 3(a), the dark pixels of each patch are marked by different colors. We pad the image repeatedly to handle the boundary issues. In the backward stage, the dark pixels of the image collect the propagating gradients of the corresponding pixels by summation.

3) **Overall Loss Function:** We combine supervised losses, unsupervised losses, and the adversarial loss to train the proposed network:

$$L = L_c + \lambda L_p + \gamma L_t + \mu L_d + \eta L_a,$$

where $\lambda$, $\gamma$, $\mu$, and $\eta$ are the positive weights of each loss function.
C. Semi-Supervised Training Details

As the supervised branch and unsupervised branch share the same architecture as well as weights, we update weights iteratively during the training process. We first randomly choose a batch of \(N_l\) labeled samples and compute the difference between dehazed images and ground-truths by labeled losses. Meanwhile, we randomly choose a batch of \(N_u\) unlabeled samples and compute the unlabeled losses. We then use the labeled/unlabeled losses to update the parameters of the supervised/unsupervised branch by back propagation, respectively. We present the training details when updating the generator in Algorithm 1.

Algorithm 1 Training Details at Each Iteration

\[ \textbf{Input:} \text{Initialized generator } G = \{G_s, G_u\}, \text{ Synthetic training data } N_l, \text{ Real training data from } N_u \]

\[ \textbf{Output:} \text{Updated generator } G. \]

1. \( \text{while } i < \text{iter}_{\text{max}} \) do
2. randomly choose hazy/clean image pair \((I, J)\) from \(N_l\)
3. randomly choose hazy image \(I_r\) from \(N_u\)
4. obtain \(J_s\) by \(J_s = G(I_s)\)
5. obtain \(J_r\) by \(J_r = G(I_r)\)
6. obtain \(L_c\) by (3) from \((J_s, J)\)
7. obtain \(L_p\) by (4) from \((J_s, J)\)
8. obtain \(L_a\) by (5) from \((J_s, J)\)
9. obtain \(L_d\) by (8) from \(J_r\)
10. obtain \(L_t\) by (6) from \(J_r\)
11. back propagate \(G_s\) by \(L_c + L_p + L_a\)
12. back propagate \(G_u\) by \(L_d + L_t\)
13. \(i \leftarrow i + 1\)
14. end while

IV. EXPERIMENTAL RESULTS

A. Implementation Details

We alternatively update the generator and discriminator by updating one while fixing the other. More specifically, we update the discriminator once after updating the generator five times. When updating the generator, we optimize the network parameters in a semi-supervised way. We use the Pytorch toolbox [25] and Adam [10] solver to optimize both the generator and discriminator. We set \(\beta_1 = 0.9, \beta_2 = 0.99\), and the weight decay as \(10^{-4}\). The network is trained for 300 epochs. The learning rate is set to be \(10^{-4}\) at the first 150 epochs, and decreased linearly to \(10^{-6}\) within the following 150 epochs by \(l_r = 10^{-4} - \frac{10^{-4} - 10^{-6}}{150}(E - 150)\), where \(E\) denotes the number of the training epoch.

We train the network by randomly choosing both labeled and unlabeled samples from the RESIDE dataset [16], which contains the ITS (Indoor Training Set), OTS (Outdoor Training Set), SOTS (Synthetic Object Testing Set), URHI (Unlabeled real Hazy Images), and RTTS (real Task-driven Testing Set). For labeled data, we select 4000 synthetic hazy images, 2000 from the ITS set and 2000 from the OTS set. For unlabeled data, we randomly choose 2000 real hazy images from the URHI dataset. We set the batch size to 4, and apply the following strategies to randomly augment the training data: 1) flipping horizontally and vertically, 2) rotating for \(-90^{\circ}\) or \(90^{\circ}\), and 3) adding Gaussian noise with the sigma of 0.01. Then we randomly crop the images to the size of \(256 \times 256\) and normalize the pixel values to \([-1, 1]\).

We set the patch size as \(35 \times 35\) when computing the DC loss. The loss weights are set as: \(\lambda = 10^{-2}, \gamma = 10^{-5}, \mu = 10^{-5}\), and \(\eta = 10^{-3}\). We train our network on an Nvidia GTX 1080 GPU and it takes three days to converge. The source code and pre-trained model will be made publicly available on the project website: https://sites.google.com/view/lerenhanli/homepage/semi_su_dehazing.

B. Evaluation Settings

We evaluate the performance of the proposed method against the state-of-the-art dehazing approaches including DCP [7], MSCNN [28], DehazeNet [2], AOD-Net [15], DCPDN [43], GFN [29], CycleGAN [4], and PDN [41]. To better understand the proposed semi-supervised method, we retrain a network which only contains the supervised branch as the baseline model. For fair comparisons in the loss function, we apply all the proposed loss function (10) on the labeled data including supervised and unsupervised losses.

C. Evaluations on Synthetic Datasets

We use three benchmark datasets [16], [44] to evaluate the proposed method, including RESIDE-C, HazeRD, and SOTS datasets. The RESIDE-C dataset contains 100 indoor and 100 outdoor synthetic hazy images randomly chosen from
the ITS and OTS databases. We note the selected images do
not appear in our training data. As shown in Figure 4 and
Table IV, the proposed method generates results with cleaner
structures and details.

We then evaluate our method on the HazeRD [44] and
SOTS [16] datasets. As shown in Figure 5-6 and Table IV,
our algorithm performs favorably against the state-of-the-art
dehazing methods.

We note that the network trained only with unpaired
data [4] does not perform well due to the limited learning
capability on the unlabeled data. Furthermore, the baseline
model (i.e., purely supervised) performs slightly better than
the proposed semi-supervised model in terms of PSNR on the
RESIDE-C dataset. However, the baseline does not perform as
robustly as the proposed algorithm on each synthetic dataset.
The proposed semi-supervised method can be well generalized
to the images where the image categories and scenes are
different from the training dataset.

**D. Evaluations on Real Images**

We evaluate the proposed method against the state-of-the-
art approaches on real hazy images. Figure 7 shows that our
method recovers cleaner and visually more pleasing images
than the state-of-the-art approaches. To better understand the performance of our method on real images, we apply a task-driven evaluation presented by Li et al. [16]. We test our method on the RTTS [16] dataset, which contains 4322 real-world images annotated with object categories and bounding boxes. After restoring the clean images, we apply a pre-trained Faster R-CNN [26] to detect objects of interests, and compute the mean Average Precision (mAP) of each method. Table V shows the proposed method performs favorably against the other approaches for object detection on the RTTS dataset.

The proposed method outperforms the baseline (i.e., purely supervised) model in both visual and task-driven evaluations. This shows that the proposed semi-supervised method is effective in learning the domain gap between synthetic data and real-world images, thus alleviating the over-fitting problems.

E. Run Time

We evaluate the run time of the proposed algorithm with comparisons to the other approaches. We randomly sample 100 hazy images of $512 \times 512$ pixels and compute the average processing time of each method. All the methods are carried out on a desktop computer with an Intel(R)
Fig. 7. Dehazed results on real hazy images. Our results are cleaner and look more pleasing.

Xeon(R) CPU E5-2670 v3@2.30GHz, 32 GB RAM, and an Nvidia GTX 1080 GPU. As DCP is based on a conventional optimization method, we evaluate the execution time on the CPU without any GPU acceleration. As shown in Table VI, our method performs competitively with state-of-the-art approaches.
Fig. 8. Sensitivity to the amount of unlabeled data. With the increasing of the unlabeled data, the result looks more pleasing.

TABLE IV
Quantitative Evaluations (PSNR/SSIM) on Three Benchmark Datasets [16]. Our Method Performs Favorably Against the State-of-the-Art Dehazing Algorithms

<table>
<thead>
<tr>
<th>Method</th>
<th>PSNR/SSIM</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(ResIDE-C)</td>
</tr>
<tr>
<td>Haze</td>
<td>14.00/0.59</td>
</tr>
<tr>
<td>DCP [7]</td>
<td>14.60/0.75</td>
</tr>
<tr>
<td>MSCNN [28]</td>
<td>17.54/0.81</td>
</tr>
<tr>
<td>DehazeNet [2]</td>
<td>20.06/0.83</td>
</tr>
<tr>
<td>AOD-Net [15]</td>
<td>18.33/0.82</td>
</tr>
<tr>
<td>DCPDN [43]</td>
<td>19.19/0.82</td>
</tr>
<tr>
<td>GFN [29]</td>
<td>19.85/0.80</td>
</tr>
<tr>
<td>PDN [41]</td>
<td>18.93/0.84</td>
</tr>
<tr>
<td>CycleGAN [4]</td>
<td>17.33/0.57</td>
</tr>
<tr>
<td>baseline</td>
<td>23.54/0.90</td>
</tr>
<tr>
<td>Ours</td>
<td>23.15/0.91</td>
</tr>
</tbody>
</table>

TABLE V
Object Detection Results on the RTTS [16] Dataset. We Apply Faster R-CNN to Detect Objects of Interests on Dehazed Images. Faster R-CNN is Trained on the VOC2007 [5] Dataset. The Detection Task Favors the Proposed Method Most Among the Other Algorithms

<table>
<thead>
<tr>
<th>Method</th>
<th>mAP (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hazy</td>
<td>37.58</td>
</tr>
<tr>
<td>DCP [7]</td>
<td>40.58</td>
</tr>
<tr>
<td>MSCNN [28]</td>
<td>41.34</td>
</tr>
<tr>
<td>DehazeNet [2]</td>
<td>40.54</td>
</tr>
<tr>
<td>AOD-Net [15]</td>
<td>37.47</td>
</tr>
<tr>
<td>GFN [29]</td>
<td>58.11</td>
</tr>
<tr>
<td>DCPDN [43]</td>
<td>61.28</td>
</tr>
<tr>
<td>PDN [41]</td>
<td>62.30</td>
</tr>
<tr>
<td>CycleGAN [4]</td>
<td>42.53</td>
</tr>
<tr>
<td>baseline</td>
<td>55.27</td>
</tr>
<tr>
<td>Ours</td>
<td>62.61</td>
</tr>
</tbody>
</table>

V. Analysis and Discussions

We analyze the proposed method with ablation studies in this section.

A. Semi-Supervised Learning

As our network architecture includes a supervised branch as the baseline, it is of great interest to understand how the semi-supervised learning formulation facilitates dehazing the images. As shown in Section IV, the proposed semi-supervised learning method helps to remove haze from real-world images while the baseline method with purely supervised learning is less effective (Table V and Figure 7). We note that the method with supervised learning can generate clean images on the synthetic test dataset which is generated in the same way as the training dataset. However, this method does not effectively remove haze from real images. This confirms our analysis that the method with supervised learning is usually limited to specific synthetic training datasets. To better understand the effectiveness of semi-supervised learning, we train the proposed network on different number of the labeled samples and evaluate it against the baseline model. Specifically, when training the supervised branch network, we use 4000, 2000, and 1000 labeled samples and use the same number (i.e., 2000) of unlabeled samples to train the unsupervised branch. For fair comparisons, we use 2000 labeled samples to train an unsupervised branch in the baseline model. For evaluation on dehazing real images, we use the RTTS [16] dataset to compute the mAP (%) on the dehazed results of each model. As shown in Table VII, the proposed semi-supervised method performs more robustly than the baseline model.
Fig. 9. Visual comparisons on different labeled losses. The combination of all labeled losses leads to a better result.

<table>
<thead>
<tr>
<th>TABLE VIII</th>
<th>QUANTITATIVE EVALUATIONS WITH DIFFERENT AMOUNT OF LABELED DATA. THE PERFORMANCE ON THE SYNTHETIC DATASET ARE ROBUST WHILE THE PERFORMANCE ON THE REAL DATASET ARE SENSITIVE TO THE UNLABELED DATA</th>
</tr>
</thead>
<tbody>
<tr>
<td>Amount of the unlabeled data</td>
<td>SOTS (PSNR/SSIM)</td>
</tr>
<tr>
<td>0</td>
<td>23.65/0.86</td>
</tr>
<tr>
<td>500</td>
<td>24.37/0.88</td>
</tr>
<tr>
<td>1000</td>
<td>24.41/0.89</td>
</tr>
<tr>
<td>2000</td>
<td>24.44/0.89</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>TABLE IX</th>
<th>QUANTITATIVE RESULTS ON DIFFERENT LABELED LOSS FUNCTIONS. THE COMBINATION OF ALL THE LABELED LOSSES PERFORMS WELL AGAINST THE OTHER ALTERNATIVES</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>PSNR</td>
</tr>
<tr>
<td>$L_c$ only</td>
<td>23.99</td>
</tr>
<tr>
<td>$L_p$ only</td>
<td>21.56</td>
</tr>
<tr>
<td>$L_c + L_p$</td>
<td>24.43</td>
</tr>
<tr>
<td>$L_c + L_p + L_a$</td>
<td><strong>24.44</strong></td>
</tr>
</tbody>
</table>

Furthermore, we evaluate the sensitivity to the amount of unlabeled data. Specifically, when training the unsupervised branch, we apply 0, 500, 1000, and 2000 unlabeled samples and use the same amount (i.e., 4000) of labeled samples to train the supervised branch. We note that the proposed method training without unlabeled data degrades to a supervised learning approach. We quantitatively evaluate the proposed method on the synthetic dataset (i.e., SOTS) and the real-world image dataset (i.e., RTTS). As shown in Table VIII, the proposed model performs similarly on the synthetic dataset while the performance on the real dataset becomes better with the amount of unlabeled data increasing. Figure 8 shows the visual results with the different amount of unlabeled training data. The proposed network performs less effectively when training with fewer unlabeled samples.

B. Supervised Losses

We analyze the effect of each supervised loss on the SOTS dataset. We fix the unlabeled losses (i.e., TV loss and DC loss) in the unsupervised branch and evaluate the proposed method using three labeled losses. As shown in Table IX and Figure 9, the method using the combination of MSE, perceptual, and adversarial losses performs well against the other alternatives.

C. Unsupervised Losses

As the performance of the unsupervised learning branch is constrained by the loss functions, we analyze the effect of each component. For fair comparisons, we fix the labeled loss functions in the supervised branch and evaluate the effect of each unlabeled loss by removing one while keeping the other one. We retrain the network with the same training dataset as presented in Algorithm 1 and quantitatively evaluate the performance on the SOTS and RTTS dataset. Table X shows that the combination of $L_d$ and $L_t$ generates better results. Solely using $L_c$ or $L_p$ in the proposed model introduces over-smooth results (Figure 9(b)) and checkerboard artifacts (Figure 9(c)), respectively. Using $L_d$ in the proposed method facilitates generating the results visually more pleasing and closer to real images.

Solely using $L_c$ or $L_p$ in the proposed model introduces over-smooth results (Figure 9(b)) and checkerboard artifacts (Figure 9(c)), respectively. Using $L_d$ in the proposed method facilitates generating the results visually more pleasing and closer to real images.

C. Unsupervised Losses

As the performance of the unsupervised learning branch is constrained by the loss functions, we analyze the effect of each component. For fair comparisons, we fix the labeled loss functions in the supervised branch and evaluate the effect of each unlabeled loss by removing one while keeping the other one. We retrain the network with the same training dataset as presented in Algorithm 1 and quantitatively evaluate the performance on the SOTS and RTTS dataset. Table X shows that the combination of $L_d$ and $L_t$ generates better results. Solely using $L_d$ or $L_t$ tends to introduce undesirable artifacts in the dehazed images as shown in Figure 10. More specifically, only using $L_d$ does not generate clean images since simply constraining the sparsity on the dark channel tends to generate artifacts with dark pixels as shown in Figure 10(b). On the other hand, the scheme of only using $L_t$ is less effective as this constraint smooths image details. Although the quantitative results decrease, they are still comparable with state-of-the-art dehazing approaches. We note that the model without using any loss function in the unsupervised branch is degraded to a supervised model, which is the same as the one in Table VIII of Section V-A. Our baseline model performs slightly lower than the full model in terms of PSNR and SSIM. The main reason is that we apply the proposed unlabeled losses on the supervised branch, which also demonstrates the effectiveness of the proposed unlabeled loss functions.
Fig. 10. Visual comparisons on different unlabeled loss functions. The combination of DC and TV losses leads to a better result.

Fig. 11. Sensitivity analysis on the four positive weights, $\lambda$, $\gamma$, $\mu$, and $\eta$ in the loss function. The proposed method is insensitive to changes in these hyper-parameters within a sensible range.

Fig. 12. Visual results on a noisy hazy image (noise level: 10%). The proposed method can remove the haze as well as image noise.

### TABLE XI

<table>
<thead>
<tr>
<th>ANALYSIS ON DIFFERENT TRAINING STRATEGIES, THE PROPOSED MODEL PERFORMS WELL AGAINST THE OTHER ALTERNATIVES</th>
</tr>
</thead>
<tbody>
<tr>
<td>PSNR</td>
</tr>
<tr>
<td>w/o skip connection</td>
</tr>
<tr>
<td>w/o residual learning</td>
</tr>
<tr>
<td>skip conn. via concat.</td>
</tr>
<tr>
<td>our full model</td>
</tr>
</tbody>
</table>

### D. Hyper-Parameters

There are four hyper-parameters in the proposed method ($\lambda$, $\gamma$, $\mu$, and $\eta$ in the loss function (10)). For sensitivity analysis, we evaluate the proposed model by varying one hyper-parameter while fixing the others. We retrain the proposed network with the same training data as mentioned in Section IV-A and compute the PSNR values on the RESIDE-C dataset. The results in Figure 11 demonstrate that the proposed method is insensitive to changes in these parameters within a sensible range.

### E. Network Architecture

To better understand the effect of each component in the proposed network, we conduct several ablation studies to analyze several design choices. Specifically, we compare the proposed network with the following models: i) without skip connections between the encoder and decoder, ii) without residual learning, iii) using concatenation instead of summation to skip connect the encoder and the decoder. Table XI shows that all these network designs are crucial to the performance of the proposed model. The model with skip connections reuses the features from the encoder, which facilitates the training on deep networks. The residual learning ensures the network focuses on predicting the details instead of the pixel values. Finally, the proposed model performs slightly better than the scheme using concatenation as the skip connection, so we choose the summation as the skip connection.

### F. Additive Noise

We use the RESIDE-C dataset to evaluate the proposed method against noise by adding random Gaussian noise of 0.5% to 10% to all the test images. We note that DCPDN [43] does not apply noise for data augmentation during the training process. In order to compare our method with DCPDN fairly, we retrain the proposed model without adding noise in the training data. As shown in Figure 13, the proposed method consistently performs well even when the noise level is high. Furthermore, adding noise to the training data can improve the
Fig. 13. Quantitative evaluations in terms of PSNR on different noise levels. Our method consistently performs better than the other algorithms [29], [43] at each noise level.

Fig. 14. Limitations on a severe hazy image. The propose method cannot effectively recover the structures and details when the image suffers from the severe haze.

G. Limitations

Figure 14 shows that our approach performs less effective when the image suffers from severe haze. In order to systematically understand the performance of the proposed method under different concentrations of image haze, we randomly select 10 clean images from the SOTS dataset and generate synthetic hazy images by the atmospheric model (1). We generate different haze concentrations by using different $\beta$ (from 0.05 to 0.5 with an interval of 0.05). Then, we evaluate the performance of the proposed method and compare it with the state-of-the-art approaches (DCP [7] and GFN [29]) on 100 synthesized hazy images in terms of PSNR. As shown in Figure 15, although all the methods do not perform robustly with the increasing of hazy concentration, the proposed semi-supervised method obtains higher PSNR values than the competitors. Our future work will focus on removing severe haze by transferring sharp scenes into hazy images from clean pictures.

VI. CONCLUSION

In this work, we propose a novel semi-supervised learning algorithm for single image dehazing as the feature domains of the synthetic and real-world images are different. On the one hand, we use labeled loss functions to train the supervised branch on the synthetic data with ground-truth labels. On the other hand, we train the unsupervised branch with real data and unlabeled loss functions based on commonly used image priors including dark channel and total variation. Extensive experimental results demonstrate that the proposed algorithm performs favorably against the state-of-the-art dehazing methods both on synthetic and real hazy images.

REFERENCES


Lerenhan Li received the B.Eng. degree from the School of Artificial Intelligence and Automation, Huazhong University of Science and Technology, where he is currently pursuing the Ph.D. degree with the School of Artificial Intelligence and Automation, supervised by Prof. N. Sang. He was a joint-training Ph.D. student with the Department of Electrical Engineering and Computer Science, University of California at Merced, supervised by Prof. M.-H. Yang. His current research interests focus on low level computer vision problems and deep learning.

Yunlong Dong received the B.Eng. degree from the School of Artificial Intelligence and Automation, Huazhong University of Science and Technology, where he is currently pursuing the Ph.D. degree with the School of Artificial Intelligence and Automation, supervised by Prof. Y. Yuan. His current research interests focus on low level computer vision problems and deep learning.

Wenqi Ren received the Ph.D. degree from Tianjin University in 2017. From 2015 to 2016, he was a joint-training Ph.D. student in electrical engineering and computer science at the University of California, Merced, CA, USA. He is currently an Assistant Professor with the Institute of Information Engineering, Chinese Academy of Sciences, China. His research interests include image/video analysis and enhancement, and related vision problems.
Jinshan Pan received the Ph.D. degree in computational mathematics from the Dalian University of Technology, China, in 2017. He was a joint-training Ph.D. student with the School of Mathematical Sciences and Electrical Engineering and Computer Science, University of California, Merced, CA, USA, from 2014 to 2016. He is currently a Professor with the School of Computer Science and Engineering, Nanjing University of Science and Technology. His research interest includes image deblurring, image/video analysis and enhancement, and related vision problems.

Changxin Gao received the Ph.D. degree in pattern recognition and intelligent systems from the Huazhong University of Science and Technology in 2010. He is currently an Associate Professor with the School of Artificial Intelligence and Automation, Huazhong University of Science and Technology. His research interests are pattern recognition and surveillance video analysis.

Nong Sang received the Ph.D. degree in pattern recognition and intelligent control from the Huazhong University of Science and Technology in 2000. He is currently a Professor with the School of Artificial Intelligence and Automation, Huazhong University of Science and Technology. His research interests include pattern recognition, computer vision, and neural networks.

Ming-Hsuan Yang (F’19) received the Ph.D. degree in computer science from the University of Illinois at Urbana-Champaign, Champaign, IL, USA, in 2000. He is currently a Professor of electrical engineering and computer science with the University of California, Merced, CA, USA. He received the NSF CAREER Award in 2012, and the Google Faculty Award in 2009. He is a Senior Member of the ACM.