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DIRECTORATE OF OPERATIONS
FLIGHT CONTROL SYSTEMS DEPARTMENT

ESATAN: AN EVALUATION

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DOCUMENT APPROVAL

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DOCUMENT CHANGE RECORD

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ABSTRACT

This paper¹ presents ESATAN, the new ESA thermal network analysis program. A description of its main features and structure is given, as well as an outline of the mathematical algorithms involved. One simple example of use is given. Finally, the program is briefly discussed from the user's point of view and its performance evaluated.

Questions, comments, suggestions, death threats etc. are welcome.

Miguel Á. Carreira Perpiñán ☺
Darmstadt, March 1994

¹ This report has been elaborated under the sponsorship of the Dirección General de Investigación Científica y Técnica (Spain).

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GLOSSARY OF TERMS

- CGM:** Computer Graphics Metafile. A widespread vector graphics format.
- DTIMEI:** input timestep for transient solution routines (ESATAN control constant).
- DTIMEU:** timestep length for a transient solution routine (ESATAN control constant).
- ESATAN:** ESA Thermal ANalyser. Program reviewed in this note.
- GKS:** Graphical Kernel System. A standard set of graphics primitives.
- Input deck, source deck:** text file containing a specification for a thermal mathematical model.
- LOG file:** file produced by the VMS operating system. It contains statistical data about the execution of a task (elapsed time, CPU time, page faults...).
- Mortran:** ESATAN-proprietary superset of Fortran 77. It includes structured constructs (SELECT...CASE, WHILE...ENDWHILE and REPEAT...UNTIL), subscripted values, etc.
- Steady state:** state that a (thermal) system reaches when time goes to infinity. It does not always exist.
- Transient:** evolution of a (thermal) system during a given time interval.
- NLOOP:** maximum number of iterations of a solution routine (ESATAN control constant).
- OUTINT:** output interval (ESATAN control constant).
- RELXCA:** convergence threshold of a solution routine (ESATAN control constant).
- SOHO:** SOLar and Heliospheric Observatory. Satellite for which a validated ESATAN source deck was available.
- TIMEND:** time at end of transient (ESATAN control constant).

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1 INTRODUCTION

ESATAN (*ESA Thermal Analyser*) is, as stated in the User's Manual, a software package for the prediction of temperature distributions in engineering components and systems using the thermal network analysis technique.

It is intended to replace ESA's former thermal analysis program, SINDA. It has been developed by the Engineering Research Centre of GEC Alsthom, Whetstone, using Fortran 77 to ANSI Standard X-3.9 1978 and it should run on any computer supporting such a compiler with only minor changes dependant on the operating system (file naming rules...).

The development and simulation of a thermal model with ESATAN involves three stages:

- Creation by the user of an input deck, that is, a text file containing, in **Mortran**² language, a specification for the model (definition of the model topology, associated tables of information regarding material properties, variation of model parameters with time, etc.) and instructions for the solution procedure.
- Preprocessing this input deck by the ESATAN preprocessor. This means checking whether the model is both syntactically and semantically consistent and then, if it is, creating a file in ESATAN's binary notation for this model as well as a Fortran program. These files are internal to ESATAN and the user should not be concerned about them. All errors occurred during the preprocess are logged onto a listing file.
- Solving the model. The former Fortran source program is compiled and linked with the system libraries plus ESATAN's own library. The resulting executable file is automatically run and its output sent to a text file which is the desired solution³. The EXE file may be run as often as desired.

The sequence of operations is very similar to that of editing, compiling and running a program.

Deriving a network model from a specified physical system is, of course, the part which requires most work for the user.

² Mortran is an ESATAN-proprietary superset of Fortran 77. It includes structured constructs (SELECT...CASE, WHILE...ENDWHILE and REPEAT...UNTIL), subscripted values, etc.

³ Basically, a solution consists of a snapshot with the predicted temperatures throughout the system. Such snapshots can be taken at intervals, thus giving a view of the evolution of the system (its transient state). When time goes to infinity the system may reach a steady state; this steady-state solution can also be calculated by ESATAN.

2 STRUCTURE OF ESATAN

ESATAN itself consists of three major components:

- The **Syntax Checker**: a fast, preliminary program to check the correctness of the syntax of a source deck. It is intended to reduce the edit-preprocess-edit cycle, as the preprocessor takes a considerable time to run for moderate to large sized input decks (see some sample preprocessing times under the epigraph *Performance Evaluation*). It won't detect every error, only the simpler ones.
- The **Preprocessor**: reads an input deck, checks it for consistency and translates it into a Fortran program.
- The **Library**: a collection of object modules which can be called from the instructions section of a user input deck.

This structure is depicted in fig. 1.

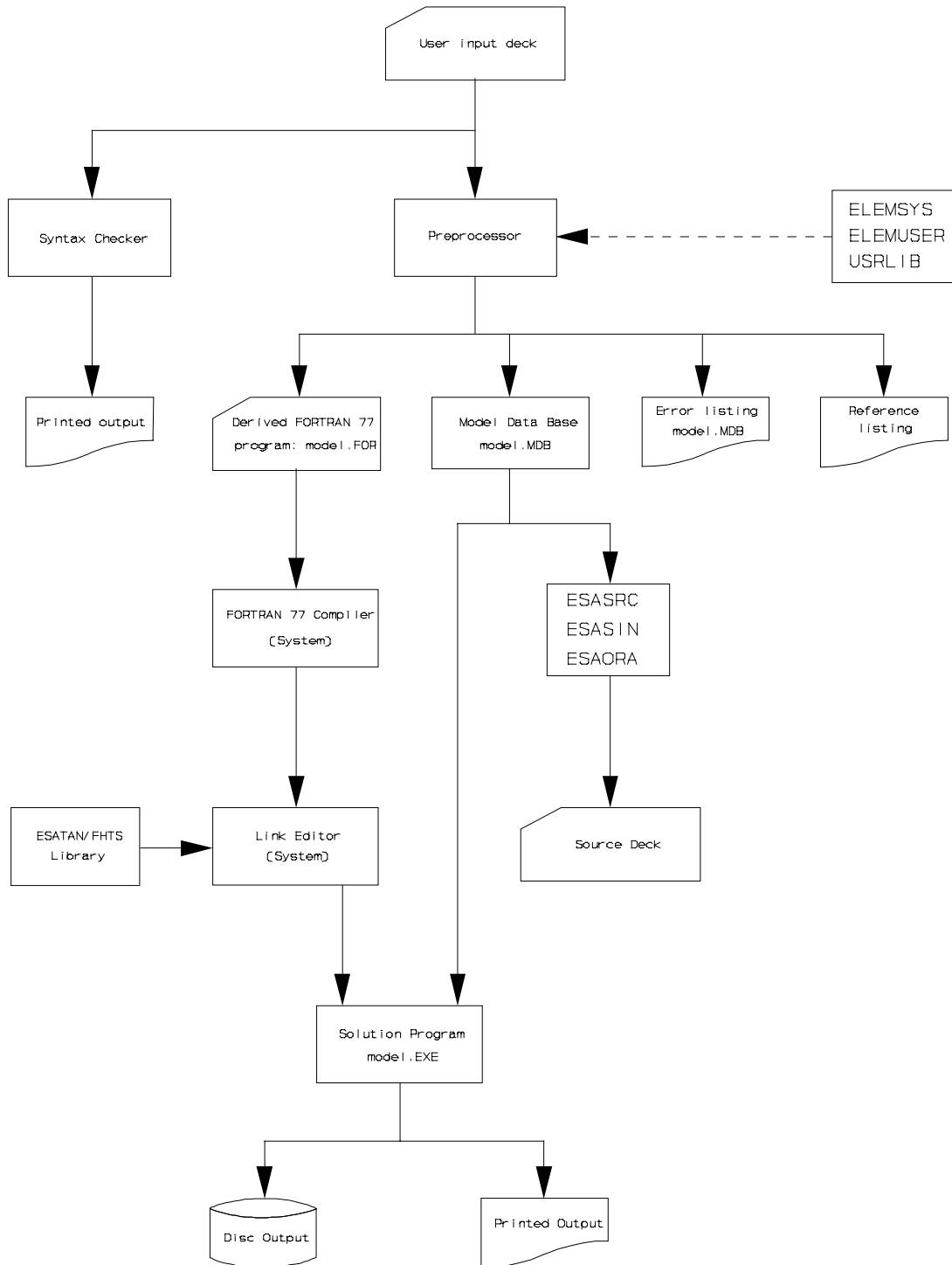


Figure 2: The Basic ESATAN System

3 THE "LUMPED PARAMETER" METHOD

The key idea in this method is to model a continuous medium as a discrete network of **nodes** (representing the capacitance of a particular section of the system) linked by **conductors** (representing its conductance). All the physical parameters of the thermal system, which are spatially distributed in it, are "lumped" in a set of quantities and assigned to each node or conductor. This means that a node or conductor is considered as a black box defined by its temperature, capacitance, etc. considered as constant throughout this node or conductor. This introduces a discretisation error which will be small if the network is fine. In the numerical algorithm, governing differential equations are approximated by means of first-order finite differences.

There is a thermal/electric analogy in which temperature equates to voltage and heat flow to current flow. The equivalent for a thermal network is an electric circuit.

3.1 The General Lumped Parameter Method Equations

This section is intended to give to the interested reader a rough, summarised idea of the underlying mathematics of thermal modelling.

Given a network with n nodes $i = N_1, \dots, N_n$, each having temperature T_i , heat capacity C_i and containing a heat source Q_i ; and being K_{ij} the linear conductance (conduction, convection and other linear processes such as evaporation or condensation) and R_{ij} the radiative exchange constant between nodes N_i and N_j ; then, applying a heat balance to node i and taking into account the heat diffusion equation⁴ and the Stefan-Boltzmann law⁵, one can see that, for $i = 1, \dots, n$:

⁴ The heat diffusion differential equation, which gives the variation of temperature with time, is

$$\frac{\partial T}{\partial t} = \alpha \nabla^2 T, \quad \alpha = \frac{\kappa}{\rho c}$$

or, in the form of Fourier's law

$$\mathbf{q} = -\kappa \nabla T = \frac{Q}{A}$$

where q is the heat flow (W m^{-2}), Q is the rate of heat transfer (W), A is the area for heat transfer, and α , κ , c and ρ are the thermal diffusivity ($\text{m}^2 \text{s}^{-1}$), thermal conductivity ($\text{W/m} \cdot ^\circ\text{C}$), specific heat ($\text{J/kg} \cdot ^\circ\text{C}$) and density (kg m^{-3}) of the material, respectively. ∇ is the nabla operator and ∇^2 is the laplacian operator.

⁵ For a grey body, the rate of radiated heat is

$$Q = \sigma \alpha \varepsilon \mathcal{F} A T^4$$

where σ is the Stefan-Boltzmann constant ($\approx 5.6697 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4$), α is the absorptivity (-), ε is the emissivity (-), \mathcal{F} is the view factor (-), A is the area of radiation (m^2) and T its temperature ($^\circ\text{C}$).

$$C_i \frac{dT_i}{dt} = \sum_{i \neq j} K_{ij} (T_j - T_i) + \sum_{i \neq j} R_{ij} (T_j^4 - T_i^4) + Q_i \quad (\text{transient case})$$

$$0 = \sum_{i \neq j} K_{ij} (T_j - T_i) + \sum_{i \neq j} R_{ij} (T_j^4 - T_i^4) + Q_i \quad (\text{steady state case})$$

In the transient case there are n coupled first-order differential equations which may be integrated numerically and in the steady state case it reduces to a non-linear system of n equations with n unknowns T_i (the system will be linear⁶ if there is no radiation present).

One needs to know the values for the thermal conductivity κ , the specific heat c , the density ρ and the geometric parameters (thicknesses, distances etc.) and then derive from them the values for the lumped parameters C_{ij} , K_{ij} and R_{ij} . A wide variety of methods may be used to achieve this, depending on the geometry and other factors.

For more information the reader is referred to the Engineering Manual of ESATAN. Examples are given there for:

- Discretising plates and cylinders;
- Calculating the associated conductances;
- Calculating view factors;

as well as pointers to the specialised literature, which provides with formulae for more complex geometries (handbooks, etc.).

⁶ If the conductivity κ varies with the temperature (which is the normal case), then the system is always non-linear.

4 ESATAN'S MAIN FEATURES

■ Allowed heat transfer types are conductive, convective and radiative, any of which can be non-linear with respect to temperature or time.

■ Physical parameters like specific heat, heat capacitance, emissivity area etc. can vary arbitrarily with temperature, time, position or other variables.

■ A number of routines are provided for:

- Both steady-state and transient solutions (there are several different methods to choose from).

- Mathematical routines: Lagrangian interpolation, approximate integration, matrix operations (including transposition, inversion and determinant evaluation), polynomial substitution, least squares fit, etc.

- Error reporting.

- Output formatting: facilities are provided to print values for the temperature, capacitance, heat sources (albedo, internal, etc.), heat flow, infrared emissivity and many other variables, as well as tables, averages, sums, maxima, balances etc.

- Plotting: X-Y arrays or one variable against time. ESATAN can produce *Computer Graphics Metafiles* (CGM) thanks to the use of the *Graphical Kernel System* (GKS).

- Others: array sort, scaling...

■ Useful physical constants like g (acceleration due to gravity) or σ (Stefan-Boltzmann) are built-in.

■ The units for all quantities are those of the *Système International d'Unités* (SI) except for temperature, which is measured by default in Celsius degrees (Kelvin, Fahrenheit or Rankine scales are possible too).

■ Models may be built in a hierarchical way: each model can in turn have several submodels, resulting in a tree structure with up to 99 levels.

■ Submodels can be combined either by node merging or by inter-model conductance links.

■ Implicit model definition by the inclusion of previously defined submodels.

- Batch editor permitting implicit model definitions to be modified.

■ The user can control the solution process (convergence, accuracy, etc.) by specifying other values than the default for certain parameters (eg. number of iterations, convergence criterion...).

- Extensions to ESATAN:

- FHTS (*Fluid Heat Transport System*): models fluid networks giving a solution for pressure, mass-flow rate and temperature/enthalpy. A library with solution routines and standard elements (pumps, condensers, etc.) is supplied, as well as a graphical front end. Boiling, condensation, melting, solidification, gas-solid transitions and other phase-change phenomena can be modelled.

- ESARAD: separate program to generate 3D thin-shell models.

- ABLAT: ablation modelling facility⁷.

■ Some commented example input decks are provided, as well as a Training Manual.

■ Also includes an ORACLE database interface which allows storing an ESATAN model in an ORACLE database (ESAORA).

■ There are utilities to translate an ESATAN input deck to/from a SINDA model (ESASIN) and to obtain an input deck from a model database (ESASRC).

⁷ Under development.

5 GENERAL STRUCTURE OF AN INPUT DECK

A source deck is made up of **blocks**. There are two types of blocks: *operations* and *data* blocks. Data blocks are used to define the topology of the network, as well as to give values to physical constants and properties. Operations blocks are used to give instructions on how the solution will be reached and what outputs will be printed.

The most important data blocks are⁸:

\$NODES: identify nodes and give initial temperature for them and, optionally, capacitance, heat sources, area, absorptivity and emissivity. Each node can belong to one of three types: diffusion, boundary (it represents a boundary condition, i.e. its temperature is constant) and inactive (they aren't taken into account in the solution).

\$CONDUCTORS⁹: define links between nodes and give the value for its conductance. There are four different types, namely linear (conduction through a solid or convection between a solid and a fluid), radiative, fluidic (one-way mass-flow) and radiative with view-factors.

\$CONSTANTS: user-defined variables and control constants like *DTIMEI* (input time step for transient solution), *RELXCA* (convergence criterion), *TIMEND* (time at end of transient solution), *NLOOP* (maximum no. of iterations), *OUTINT* (output interval), among others. Arrays of values can also be defined.

The most important operations blocks are:

\$EXECUTION: all solution and user-defined¹⁰ routines must be called from this block.

\$OUTPUTS: contains operations to be performed at each output interval (*OUTINT*) for a transient solution or at the end of a steady state solution.

A hash (#) anywhere (except inside string constants) means that the rest of the line is a comment. Lines following the **\$MODEL** line are also handled as comments until the start of the next **\$KEYWORD** line. Needless to say, one should properly comment source decks — neither too much nor too little.

⁸ Each data or operations block starts with a **\$KEYWORD** line and ends with the **\$KEYWORD** line of the following block.

⁹ Data in the **\$NODES** and **\$CONDUCTORS** blocks may be defined as literal values, variables, variable expressions or user defined functions.

¹⁰ In a **\$SUBROUTINES** block.

6 A WORKED EXAMPLE

The following example is a model of a bar insulated along its length, radiating to deep space at both ends and containing a constant heat source at one end. All material properties are constant. The bar is represented by five diffusion nodes, the two end nodes being half the volume of the three internal nodes. Deep space is represented by boundary node B10. Figure 2 shows the bar and figure 3 the derived thermal network.

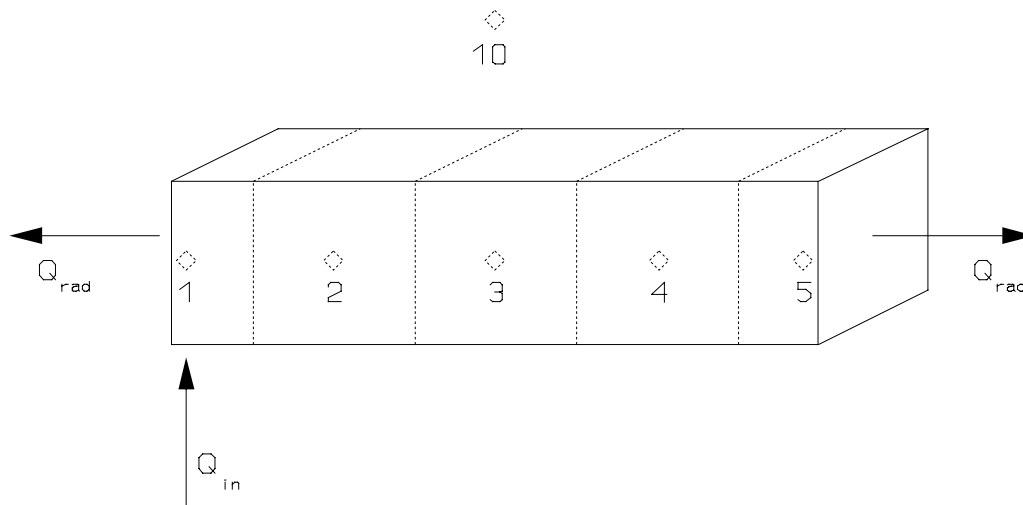


Figure 3: Bar model

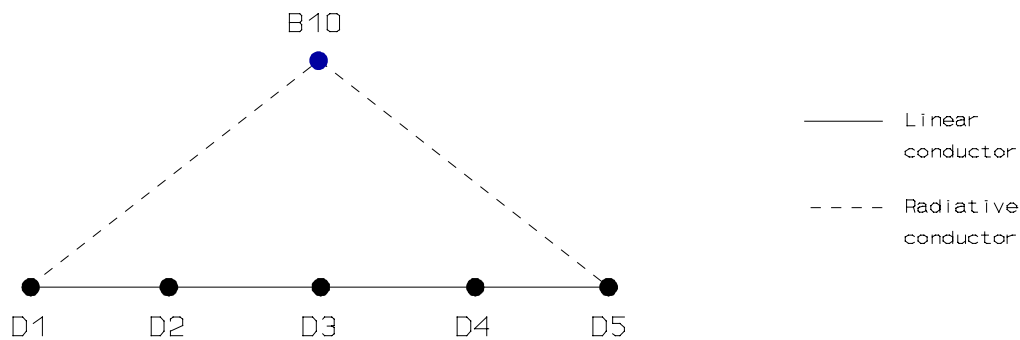


Figure 4: Derived thermal network for the bar model

The reference listing and solution output files are given following the listing of the input deck. General features of the reference listing are its standardised format, model level number and line numbering, and data block information summary. The output file contains information at the top of each file including date, time, page number and solution control constant values.

☞ Note that, in order to get some snapshots of the evolution of this system, a transient solution routine is used (*SLFRWD*) with time limit *TIMEND* = 100 seconds and output interval *OUTINT* = 30 seconds. In this case a steady state solution routine might not converge because there is a constant heat source which keeps temperature growing up with time continuously throughout the bar and this may not be balanced by radiation heat loss through both ends, thus preventing the system from reaching equilibrium¹¹.

¹¹ Running ESATAN with the *SOLVIT* solution routine shows that in this case a steady state actually exists. The following is *SOLVIT*'s output:

```
1
EUROPEAN SPACE AGENCY THERMAL ANALYSIS NETWORK (VERSION 5.5) PAGE 1
7 MARCH 1994 10:00:07 LBAR

Ejemplillo migueluno de prueba -- 09:28:00, 07/03/94

TIMEN = 0.00 MODULE SOLVIT LOOPCT = 100 ENBALA = 0.0366 ENBALR = 0.0005

TABLE OUTPUT WITH ZENTS = 'L,T'
FOR NODES OF ZLABEL = ' '
=====
+LBAR

      NODE LABEL T
      ---
1 Bar with end source 865.82
2 Bar 862.77
3 Bar 859.72
4 Bar 856.67
5 Bar end 853.61
10 -273.15
```

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6.1 Input Deck for Model LBAR

```
$MODEL LBAR
      Ejemplillo migueluno de prueba -- 09:28:00, 07/03/94
      LINEAR BAR MODEL
#
$NODES
#
D1 = 'Bar with end source',
T = 26.67, C = 38.925, QI = 70.0;
D3 = 'Bar', T = 26.67, C = 77.85;      # C = MASS * SPECIFIC HEAT CAPACITY
D2 = 'Bar', T = 26.67, C = 77.85;      # NODE NOS. NEED NOT BE IN ORDER
D4 = 'Bar', T = 26.67, C = 77.85;
D5 = 'Bar end', T = 26.67, C = 38.925;
B10, T = -273.15;
#
$CONDUCTORS
# Linear
GL(1, 2) = 11.25;
GL(2, 3) = 11.25;
GL(3, 4) = 11.25;
GL(4, 5) = 11.25;
# Radiative
GR(1, 10) = 3.75E-4;
GR(5, 10) = 3.75E-4;
#
$CONSTANTS
#
$CONTROL
#
TIMEND = 100.0;      # TIME AT END OF TRANSIENT
OUTINT = 30.0;      # OUTPUT INTERVAL
RELXCA = 0.01;      # CONVERGENCE CRITERION
NLOOP = 100;      # MAXIMUM NO. OF ITERATIONS
#
# OPERATIONS BLOCKS NEXT
#
$EXECUTION
#
      HEADER = '@(#)case01.d1.11      10:22:32,92/10/01'
      CALL SLFRWD
#
$OUTPUTS
#
      CALL PRNDB(' ', 'L,T', CURRENT)
#
$ENDMODEL LBAR
```

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6.2 Checked Listing for Model LBAR

```

@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@
@
@ ESATAN SYNTAX CHECKER @
@
@ @SYN@ - syntax error @
@ @SEM@ - semantic error @
@ @WAR@ - warning @
@
@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@@

$MODEL LBAR

      Ejemplillo migueluno de prueba -- 09:28:00, 07/03/94

      LINEAR BAR MODEL

#
$NODES
#
D1 = 'Bar with end source',
T = 26.67, C = 38.925, QI = 70.0;
D3 = 'Bar', T = 26.67, C = 77.85;      # C = MASS * SPECIFIC HEAT CAPACITY
D2 = 'Bar', T = 26.67, C = 77.85;      # NODE NOS. NEED NOT BE IN ORDER
D4 = 'Bar', T = 26.67, C = 77.85;
D5 = 'Bar end', T = 26.67, C = 38.925;
B10, T = -273.15;
#
$CONDUCTORS
# Linear
GL(1, 2) = 11.25;
GL(2, 3) = 11.25;
GL(3, 4) = 11.25;
GL(4, 5) = 11.25;
# Radiative
GR(1, 10) = 3.75E-4;
GR(5, 10) = 3.75E-4;
#
$CONSTANTS
#
$CONTROL
#
TIMEND = 100.0;      # TIME AT END OF TRANSIENT
OUTINT = 30.0;      # OUTPUT INTERVAL
RELXCA = 0.01;      # CONVERGENCE CRITERION
NLOOP = 100;      # MAXIMUM NO. OF ITERATIONS
#
# OPERATIONS BLOCKS NEXT
#
$EXECUTION
#
      HEADER = '(#)case01.d1.11      10:22:32,92/10/01'
      CALL SLFRWD

#
$OUTPUTS
#
      CALL PRNDTB(' ', 'L,T', CURRENT)
#
$ENDMODEL

LBAR

@@@ ERROR MESSAGE SUMMARY @@@

      0 syntax errors in input file
      0 semantic errors in input file
      0 warnings in input file
```

6.3 Reference Listing for Model LBAR

```

EUROPEAN SPACE AGENCY THERMAL ANALYSIS NETWORK
EEEEEEEEEEEE SSSSSSSSSS AAAAAAAAAA TTTTTTTTTT AAAAAAAAAA NN NN
EEEEEEEEEEEE SSSSSSSSSS AAAAAAAAAA TTTTTTTTTT AAAAAAAAAA NNN NN
EE SS SS AA AA TT AA AA NNNN NN
EE SS SS AA AA TT AA AA NN NN NN
EE SSS AA AA TT AA AA NN NN NN
EEEEEEEE SSSSSSSS AAAAAAAAAA TT AAAAAAAAAA NN NN NN
EEEEEEEE SSSSSSSS AAAAAAAAAA TT AAAAAAAAAA NN NN NN
EE SSS AA AA TT AA AA NN NN NN
EE SS SS AA AA TT AA AA NN NNNN
EE SS SS AA AA TT AA AA NN NNN
EEEEEEEEEEEE SSSSSSSSSS AA AA TT AA AA NN NN
EEEEEEEEEEEE SSSSSSSSSS AA AA TT AA AA NN NN
  
```

EUROPEAN SPACE AGENCY THERMAL ANALYSIS NETWORK

```

DESIGNED AND DEVELOPED: ENGINEERING RESEARCH CENTRE          SUPPORT: USERS REQUIRING SUPPORT FOR USE OF THIS
                        WHETSTONE                               PROGRAM SHOULD CONTACT:-
                        LEICESTER
                        U.K.
EUNET ADDRESS:        esatan@gec-erc.co.uk
                        CENTRAL SUPPORT: C J KIRTLEY, ERC, ... " ... " ... " ...
                        N J STOCK, ERC, (44)-533-750750 EXT 3521.
                        LOCAL SUPPORT: ADD LOCAL SUPPORT NAME HERE 0 is letter o

INSTALLATION          : ADD INSTALLATION NAME HERE 0 is zero

VERSION               : 5.5

ISSUE DATE           : APRIL 1992
  
```

```

=====
MODEL NAME           : LBAR

DATA BASE FILES:    LBAR.MDB  LBAR.FOR

RUN DATE            : 19 MAY 1993      11:20:14

EDIT NO.            : 0

ERRORS              : NONE

=====
  
```

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ESATAN REFERENCE LISTING FOR MODEL LBAR

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PAGE 1

```
0 1 $MODEL LBAR , REAL , LIST , STANDARD
0 2
0 3 Ejemplillo migueluno de prueba -- 09:28:00, 07/03/94
0 4
0 5 LINEAR BAR MODEL
0 6 #

0 7 $LOCALS
0 8 $INTEGER
0 9 $REAL
0 10 $CHARACTER

*****
$LBAR $NODES
*****

0 11 $NODES
0 12 #THERMAL
0 13 D1 = 'Bar with end source' , T = 26.67 , C = 38.925 ,
    QI = 70.0 ; D2 = 'Bar' , T = 26.67 , C = 77.85 ;
0 15 D3 = 'Bar' , T = 26.67 , C = 77.85 ;
0 16 D4 = 'Bar' , T = 26.67 , C = 77.85 ;
0 17 D5 = 'Bar end' , T = 26.67 , C = 38.925 ;
0 18 B10 , T = - 273.15 ;
0 19 #FLUID

DATA SUMMARY FOR NODES
5*DIFFUSION
1*BOUNDARY

*****
$LBAR $CONDUCTORS
*****

0 20 $CONDUCTORS
0 21 # LINEAR
0 22 GL(1 , 2) = 11.25 ; GL(2 , 3) = 11.25 ; GL(3 , 4) = 11.25 ; GL(4 , 5) = 11.25 ;
0 26 # RADIATIVE
0 27 GR(1 , 10) = 3.75E-4 ; GR(5 , 10) = 3.75E-4 ;
0 29 # FLUIDIC
0 30 # VIEW FACTOR
0 31 # LINEAR INTER-MODEL
0 32 # RADIATIVE INTER-MODEL
0 33 # FLUIDIC INTER-MODEL
0 34 # MASS
0 35 # FITTING LOSS
0 36 # MASS INTER-MODEL
0 37 # FITTING INTER-MODEL
```


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ESATAN REFERENCE LISTING FOR MODEL LBAR

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PAGE 2

```
DATA SUMMARY FOR CONDUCTORS
  4*  LINEAR
  2*  RADIATIVE

*****
$LBAR                                $CONSTANTS
*****

0  38 $CONSTANTS
0  39 #
0  40 #
0  41 $INTEGER
0  42 $REAL
0  43 $CHARACTER
0  44 $CONTROL
0  45 TIMEND = 100.0 ; OUTINT = 30.0 ; RELXCA = 0.01 ; NLOOP = 100 ;

DATA SUMMARY FOR CONSTANTS
  4*  $CONTROL

0  49 $ARRAYS
0  50 $INTEGER
0  51 $REAL
0  52 $CHARACTER
0  53 $TABLE
0  54 $SUBROUTINES
0  55 $INITIAL
0  56 $VARIABLES1
0  57 $VARIABLES2

*****
$LBAR                                $EXECUTION
*****

0  58 $EXECUTION
0  59 #
0  60     HEADER = '@(#)case01.d1.11      10:22:32,92/10/01'
0  61     CALL SLFRWD
0  62 #

*****
$LBAR                                $OUTPUTS
*****

0  63 $OUTPUTS
0  64 #
0  65     CALL PRNDB(' ', 'L,T', CURRENT)
0  66 #
0  67 $ENDMODEL LBAR

=====
```

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PAGE 3

HIERARCHY OF MODELS INCLUDING VIRTUALS(V).

LEVEL MODEL NAME

0 LBAR

===== END OF ESATAN REFERENCE LISTING FOR MODEL LBAR =====

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6.4 Output Listing for Model LBAR

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11:22:15

(VERSION 5.5)

PAGE 1
LBAR

@(#)case01.d1.11 10:22:32,92/10/01

TIMEN = 0.00 MODULE SLFRWD DTIMEU = 3.2868

CSGMIN = 3.4598 AT NODE 1 IN SUB-MODEL

LBAR

TABLE OUTPUT WITH ZENTS = 'L,T'
FOR NODES OF ZLABEL = ' '

LBAR

| NODE | LABEL | T |
|------|---------------------|---------|
| 1 | Bar with end source | 26.67 |
| 2 | Bar | 26.67 |
| 3 | Bar | 26.67 |
| 4 | Bar | 26.67 |
| 5 | Bar end | 26.67 |
| 10 | | -273.15 |

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19 MAY 1993

11:22:15

(VERSION 5.5)

PAGE 2
LBAR

@(#)case01.d1.11 10:22:32,92/10/01

TIMEN = 30.00 MODULE SLFRWD DTIMEU = 1.8527
CSGMIN = 3.4598 AT NODE 1 IN SUB-MODEL

LBAR

TABLE OUTPUT WITH ZENTS = 'L,T'
FOR NODES OF ZLABEL = ' '

=====

LBAR

| NODE | LABEL | T |
|------|---------------------|---------|
| 1 | Bar with end source | 41.25 |
| 2 | Bar | 35.91 |
| 3 | Bar | 32.22 |
| 4 | Bar | 30.08 |
| 5 | Bar end | 29.37 |
| 10 | | -273.15 |

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19 MAY 1993

11:22:15

(VERSION 5.5)

PAGE 3
LBAR

@(#)case01.d1.11 10:22:32,92/10/01

TIMEN = 60.00 MODULE SLFRWD DTIMEU = 1.8528
CSGMIN = 3.4598 AT NODE 1 IN SUB-MODEL

LBAR

TABLE OUTPUT WITH ZENTS = 'L,T'
FOR NODES OF ZLABEL = ' '

=====

LBAR

| NODE | LABEL | T |
|------|---------------------|---------|
| 1 | Bar with end source | 48.22 |
| 2 | Bar | 42.80 |
| 3 | Bar | 38.92 |
| 4 | Bar | 36.60 |
| 5 | Bar end | 35.81 |
| 10 | | -273.15 |

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EUROPEAN SPACE AGENCY THERMAL ANALYSIS NETWORK
19 MAY 1993

11:22:15

(VERSION 5.5)

PAGE 4
LBAR

@(#)case01.d1.11 10:22:32,92/10/01

TIMEN = 90.00 MODULE SLFRWD DTIMEU = 1.8528
CSGMIN = 3.4598 AT NODE 1 IN SUB-MODEL

LBAR

TABLE OUTPUT WITH ZENTS = 'L,T'
FOR NODES OF ZLABEL = ' '

=====

LBAR

| NODE | LABEL | T |
|------|---------------------|---------|
| 1 | Bar with end source | 54.94 |
| 2 | Bar | 49.51 |
| 3 | Bar | 45.63 |
| 4 | Bar | 43.29 |
| 5 | Bar end | 42.50 |
| 10 | | -273.15 |

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EUROPEAN SPACE AGENCY THERMAL ANALYSIS NETWORK
19 MAY 1993

11:22:15

(VERSION 5.5)

PAGE 5
LBAR

@(#)case01.d1.11 10:22:32,92/10/01

TIMEN = 100.00 MODULE SLFRWD DTIMEU = 1.7132
CSGMIN = 3.4598 AT NODE 1 IN SUB-MODEL

LBAR

TABLE OUTPUT WITH ZENTS = 'L,T'
FOR NODES OF ZLABEL = ' '

=====

LBAR

| NODE | LABEL | T |
|------|---------------------|---------|
| 1 | Bar with end source | 57.17 |
| 2 | Bar | 51.74 |
| 3 | Bar | 47.86 |
| 4 | Bar | 45.52 |
| 5 | Bar end | 44.73 |
| 10 | | -273.15 |

7 OUR INSTALLATION OF ESATAN

We are using ESATAN version 5.5¹² for the VAX and it is installed in our server, **SIMDS1**. Every user connected to it can execute the program. It is necessary to have Motif running under DECwindows in order to use the *FHTS Graphical Front End*. For the rest of possible actions, a text terminal is enough.

Presently, ESATAN is licensed for only one CPU (the server), so it won't run when started from a different VAXstation.

However, our installation is not complete: some modules, including ESARAD, ABLAT, ESAORA and the interfaces with window-systems are missing.

¹² Now we have version 6.3 as well.

8 USER ORIENTATION EVALUATION

■ ESATAN offers a spartan human interface, but you don't need much more anyway. The program is started by calling the command file ESATAN.COM, which in turn will call the corresponding executable image(s). The main menu is:

```

                                     ESATAN

WHICH OPTION DO YOU REQUIRE?
  SYNTAX CHECKER (C)
  PREPROCESS (P)
  SOLVE (S)
  BATCH (B)
  ESATAN SOURCE DUMP (D)
  ESATAN TO SINDA TRANSLATOR (E)
  SINDA TO ESATAN TRANSLATOR (T)
  FHTS GRAPHICAL FRONT END (G)
  QUIT (Q)
OPTION = :
```

Figure 4: ESATAN main menu

After selecting the desired option you are asked to give the appropriate file/model names.

The **S** option (*Solve*) will compile and link the FORTRAN program which resulted from the preprocess of the input deck, and furthermore it will run it thus getting the desired solution.

You can preprocess, solve or both in batch mode by selecting the **B** option (*Batch*).

The **D** option allows to get a source deck from a model database. The **E** and **T** options are useful for conversions between ESATAN and SINDA formats, although occasionally some manual corrections will be unavoidable, because they are not fully compatible.

■ Errors that occurred when using the menus are poorly described and don't even appear in the User's Manual. In general, it provides little information about how to start the program, choose options, etc. although it is quite straightforward. It would also be nice to have a printout of the initial screen (like above). The **G** option (*FHTS Graphical*

Front End) isn't documented at all.

■ The fact that ESATAN can presently be only run from the server could overload it when run from several terminals at once, especially if one takes into account that preprocessing a moderate-sized input deck is quite time-consuming (see the *Performance Evaluation* epigraph).

■ It takes little time to learn the preprocessor syntax, but designing a network for a given system requires some knowledge of thermal systems (heat transfer foundations, main equations) and even of numerical analysis if a full profit is to be obtained from the library functions.

■ Basic FORTRAN programming ability is necessary.

■ For all purposes, the **documentation** about a model should include not only the source deck, but also schematics of the associated network, showing the relation between nodes and conductors with the physical system and explaining how the significative values (constants, capacitances, etc.) were obtained (or, at least, pointing to references: thermal handbooks, etc.), as well as a justification of the chosen derived network. That is of paramount importance in big systems but should not be overlooked in the smaller ones. A glossary would be more than welcome, specially when lots of acronyms are employed.

■ Creating an input deck with a text editor is a tough task and error-prone. A graphical interface is a must.

■ ESATAN allows the user to define local constants —visible only to the preprocessor— in the **\$LOCALS** data block, but with a restricted naming: *ILn* (integer), *RLn* (real) and *ZLn* (character), where *n* is an integer. For the sake of clarity, it would be desirable to have more freedom when choosing constant names. Otherwise it is very common to end up with expressions like this one¹³:

```
GL(1,408)=1./((1./((20.0*RL701)+(0.05*8.)))+  
(2./((4.*RL314*RL106*RL153)/(LOG((RL701+A408)/(2.*RL701))))));
```

¹³ Taken from the input deck prepared for the SOHO satellite.

9 PERFORMANCE EVALUATION

9.1 Introduction

A performance study of ESATAN is presented. The reader who is only interested in the result and not in how it was reached can jump directly to appendix III.

Here the two computational phases required for carrying out a simulation with ESATAN, namely **preprocessing** an input deck and **running** the resulting executable file, are discussed in terms of performance. The CPU consumption for a number of cases is presented and then an approximate general formula derived from these data (using a least-squares fit) is given.

The numerical measures for the preprocessing and execution time were obtained by preprocessing the input deck in batch mode (option B in ESATAN's main menu) and submitting the resulting executable file to the VAX system, respectively. In both cases the elapsed CPU time (that is, the CPU time used for preprocessing or running, without the time due to other users) can be found by inspecting the corresponding LOG file¹⁴.

All the time values are given in seconds unless otherwise noted.

The actual system in which this performance evaluation was accomplished is our server, SIMDS1, a VAX 3800 rated with about 8 VUPs or some 8.4 MIPS¹⁵.

9.2 Preprocessing Performance

9.2.1 Fit model

It is advisable to have an idea at least of the order of magnitude of the time that a preprocessing pass will take. Unfortunately the examples that ESATAN provides with are all small-sized but hopefully the fit given will still produce acceptable estimates for large-sized models (more than 500 nodes).

¹⁴ Apart from other things, the LOG file gives: elapsed time (wall-clock time), CPU time and number of page faults. The VMS operating system uses virtual memory and page faults occur when a reference virtual address does not reside in RAM but on disk. The process of fetching some disk blocs (depending on the replacing strategy used) takes much longer than a RAM access. This introduces a major variability source in the time measured, as it is usually not possible to know *a priori* the average access time for a virtual memory address (it depends on the amount of memory installed, how many processes are running...).

¹⁵ Indeed, while this document was being completed our server was upgraded from a VAX 3800 rated with *around* 8 VUPs to a VAX 4100 rated with 24 VUPs (approximately 25.2 MIPS); the architecture —and thus the instruction set— are similar, so one can expect a uniform performance improvement. I carried out some tests by running exclusively either ESATAN itself (the preprocessor) or executable files created using ESATAN and the resulting relative performance turned out to be about 2.6 for the VAX 4100. The only time measures made with the new server are those belonging to the SOHO satellite input deck and they have been multiplied by the factor 2.6, so that a comparison can be done.

The input deck is supposed to consist of *definition statements* (such as the definition of nodes and conductors) and *non-definition statements* (the rest: comments, executable statements, block headers etc.). In general, it will cost more to preprocess a definition statement than a non-definition one because the latter will be normally copied to the output FORTRAN file with almost no modifications (executable statements) or even discarded (comments). It seems thus reasonable to assume that the total preprocessing time will be proportional to the size (in bytes) of each class of statements.

The variables t , s and d will designate the preprocessing time (seconds), total size of the input deck (bytes) and size of the declarative part (bytes), respectively.

☞ The reader should bear in mind that this fit is very rough and is based on weakly justified assumptions; for instance, one obvious source of variation is the loop definition of a set of nodes or links (a couple of sentences can expand to many lines, each of which defines a single node or link, thus taking much more computer time).

9.2.2 Fit formula

The experimental measures are given in appendix II (table II.1).

On the triads (s,d,t) a linear bi-dimensional fit¹⁶ was performed with the result

$$t^*(s, d) = As + Bd + C$$

$$A = 4.3 \cdot 10^{-4} \text{ s/byte} \quad B = 2.4 \cdot 10^{-4} \text{ s/byte} \quad C = 4.43 \text{ s}$$

where t^* is the fitted value of t given the values of d and s . The values of t are tabulated too for comparison with the experimental ones. The mean relative error¹⁷ is 24% while having a maximum of 61%.

9.3 Running performance

The total CPU time spent in a run for a given model depends on a number of parameters: the number of nodes, the solution routine used, the number of iterations employed globally (steady state) or in each timestep (transient), the number of timesteps (transient state), the output interval, the contents of the **\$VARIABLES1** and **\$VARIABLES2** sections... It is by far too complicated to take into account all these factors. Besides, some of them are *a priori* unknown, like the number of iterations required. It is therefore necessary to restrict oneself to a very simplified input deck.

9.3.1 Generic input deck chosen

As shown in figure 4, the skeleton input deck chosen consists of a call to the

¹⁶ See appendix I.

¹⁷ See appendix I.

SOLVIT steady-state solution routine and a call to the *PRNDTB* (*Print Data Block*) output routine at the end of the simulation. There is no restriction on the number of nodes or conductors of the model.

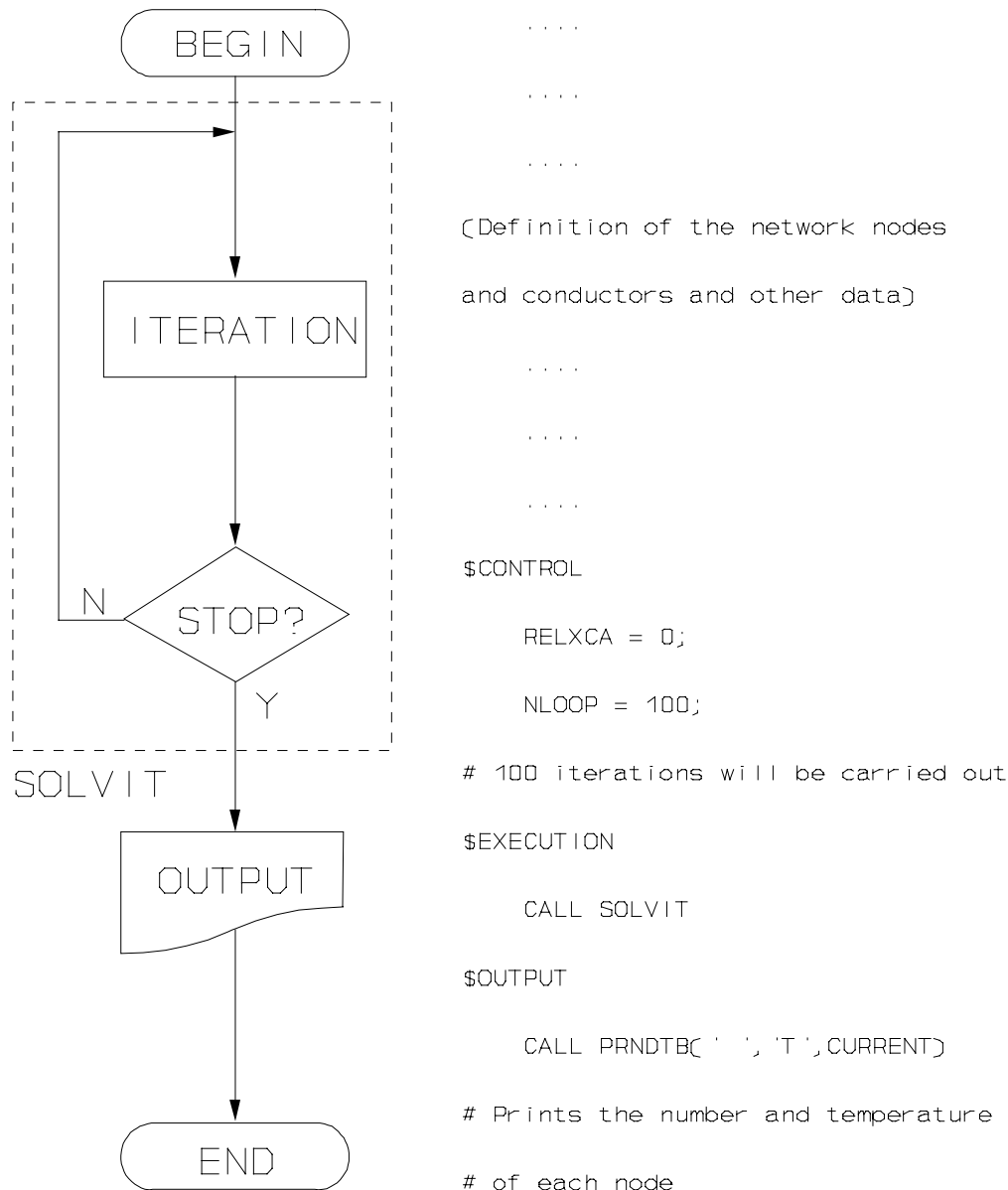


Figure 5: Skeleton source deck used for the measures

9.3.2 Fit model

The time required to simulate one of these skeleton models is equal to the time spent in the *SOLVIT* call plus the time consumed in initialising and printing the results:

1. Time spent in initialisation and output: it can be considered proportional to n because it is nothing more than printing one line per node plus a constant number of

lines. The load time of the program is almost constant, as the biggest part are the libraries (system, ESATAN...) which are linked with every model, regardless of its number of nodes. However, adding a linear dependency on c proves to improve considerably the goodness of the fit.

2. Time spent by *SOLVIT*: as shown, the *SOLVIT* routine consists basically of a loop which is repeated i times (the number of iterations). i can be easily controlled by setting the *RELXCA* control variable (convergence criterion: minimum difference in absolute value between consecutive temperatures for each node) to a very small value or just 0 (so that a lot of iterations will probably be necessary) and the setting the *NLOOP* control variable (maximum number of iterations allowed) to the actual number of iterations desired.

The time spent in each iteration, t_i , can be assumed constant for n, c fixed. Then the complexity in time of the *SOLVIT* routine will be linear in i .

So far the complexity in time for the skeleton model has the form:

$$t^*(n, c, i) = t_i(n, c) i + t_o(n, c)$$

For t_o we proposed above a linear dependency on n and c :

$$t_o(n, c) = \epsilon n + \zeta c + \eta$$

This hypothesis was contrasted with experimental data¹⁸ and the following values found for a linear-2D regression fit: $\epsilon = 2.6 \cdot 10^{-3}$ s, $\zeta = 1.2 \cdot 10^{-4}$ s, $\eta = 0.93$ s, with $\epsilon = 5\%$ and $\epsilon_{\max} = 12\%$.

Now, we propose the following dependency of t_i (time per iteration) on n and c :

$$t_i(c, n) = \alpha c + \beta n^2 + \gamma n + \delta$$

That is, linear in c and quadratic in n . Both theoretical considerations and experimentation lead to this decision. Each iteration must deal with $n \times n$ matrices which are mostly composed of zeroes (they are **sparse matrices**). A conductor between nodes (i, j) will make elements (i, j) and (j, i) different from zero in a certain matrix; otherwise they will be zero, which is the case for most pairs (i, j) as not every node will be connected to all the remaining nodes in a real system. ESATAN seems to use a sparse matrix algorithm for some operations (that is, dependant linearly on the number of non-zero elements: in other words, c) and a normal one for others (dependant quadratically on n). Thus the expression above for t_i .

A regression fit was performed on it¹⁹ with the data given in table II.2²⁰. The

¹⁸ Shown in appendix II.

¹⁹ See appendix I.

²⁰ See appendix II.

residuals are $\alpha = 10^{-4}$ s, $\beta = 4 \cdot 10^{-7}$ s, $\gamma = 7.5 \cdot 10^{-5}$ s, $\delta = 0$ s with error bounds $\varepsilon = 7\%$ and $\varepsilon_{\max} = 29\%$.

9.3.3 Fit formula

The time needed to run a skeleton model can be approximated as:

$$t(n, c, i) = (\alpha c + \beta n^2 + \gamma n + \delta) i + \varepsilon n + \zeta c + \eta$$

where $\alpha = 10^{-4}$, $\beta = 4 \cdot 10^{-7}$, $\gamma = 7.5 \cdot 10^{-5}$, $\delta = 0$, $\varepsilon = 2.6 \cdot 10^{-3}$, $\zeta = 1.2 \cdot 10^{-4}$, $\eta = 0.93$ (all the parameters are in seconds).

The error bounds for t are: $\varepsilon = 5\%$, $\varepsilon_{\max} = 16\%$.

9.3.4 When is the former formula accurate?

For small or medium thermal models, the fit will produce good predictions as long as the models are kept "simple." It will underestimate the running time with, for example:

- Models that present high non-linearities, which oblige ESATAN to make interpolations on different magnitudes as a function of the temperature.

- Use of certain features which are computationally very expensive: *VCHP* (Variable Conductance Heat Pipe Control), *VFAC* (computation of radiative conductances for a view factor submodel), etc.

- ...

As the biggest model that the author could have access to has only 208 nodes, it is unknown whether the formula will still give proper values for big models (more than 500 nodes).

Nevertheless, it is hoped that it will be an acceptable estimate of at least the order of magnitude of the running time.

9.3.5 Performance of ESATAN for transient-state simulations

Essentially, what ESATAN does to dynamically calculate the nodal temperatures is to update them periodically. The time interval between updates, called **timestep**, must be small enough so that the required accuracy is attained. The whole simplified process is depicted in figure 5.

The timestep length, *DTIMEU*, is computed internally by ESATAN as

²¹ The model *NLBAR* was discarded because it is a clear outlier. This is due to the high non-linearities that it contains: 85% of the nodes and 50% of the conductors interpolate material properties such as heat capacity or conductivity as a non-linear function of temperature and this takes more computer time when compared with the rest of the models used, which are quite linear.

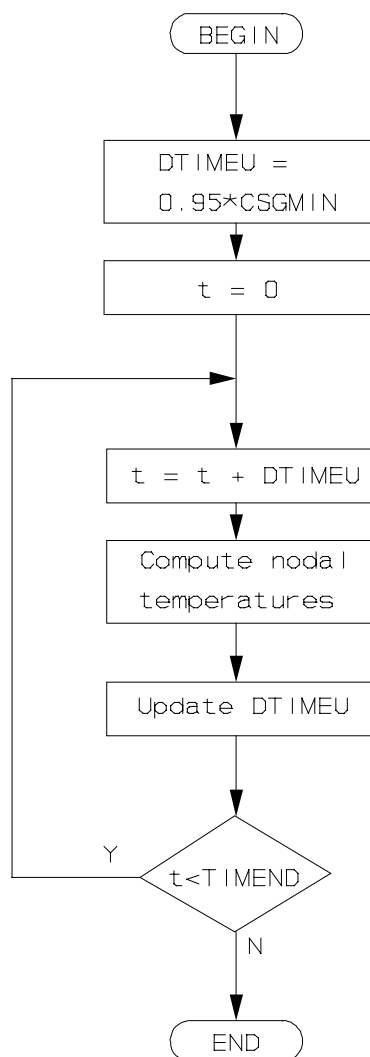


Figure 6: Transient-state simulation with ESATAN

$$DTIMEU = 0.95 * CSGMIN$$

$$CSGMIN = \min_{i=1, \dots, n} \left\{ \frac{C_i}{\sum_{j \neq i} GL_{ij}} \right\}$$

where C_i is the heat capacitance of node i and GL_{ij} is the heat conductance of the link between nodes i and j . The expression

$$\frac{C_i}{\sum_{j \neq i} GL_{ij}}$$

has units of time and has the same physical meaning as $1/\tau = RC$ in a resistor-capacitor circuit: it is the time constant of a "thermal circuit." It has got a different value for each node and then one must take the smallest one to satisfy all them (thus the *min* of *CSGMIN*). The 0.95 factor gives some security slack.

The timestep length does not remain constant during the simulation because the C_i and GL_{ij} can vary with time. Therefore, it must be recalculated at the end of each timestep.

ESATAN provides with five different solution routines for the transient state. They differ in how they obtain the nodal temperatures for a new timestep (using forward differences, the Crank-Nicholson method, a predictor-corrector method...). Most of these methods operate by solving an $n \times n$ system of equations iteratively, that is, the same approach used for the steady-state solution routines.

Then, knowing the number of iterations employed in each timestep one can find the total number of iterations and roughly approximate the running time with the fit formula given above (as n and c are already known).

The problem, of course, is: how does one know a priori the number of iterations? The answer is: it is almost impossible, because it depends on the mathematical nature of the matrices involved —as well as on the desired degree of accuracy (*RELXCA*, *NLOOP*).

The best thing one can do is to consider a constant timestep of $0.95 * CSGMIN$ as it is at the beginning (this relies on the fact that the material properties relevant for heat transfer won't usually change too much with temperature, which is a good assumption) and take an "average" number of iterations per timestep, \bar{I} . Then, the following expression will yield the grand total of iterations for the whole simulation:

$$i = \frac{TIMEND}{0.95 \times CSGMIN} \times \bar{I}$$

where the number of timesteps is

$$\frac{TIMEND}{0.95 \times CSGMIN}$$

(*TIMEND* is the time at the end of the transient state).

Alternatively, one can just leave unknown the number of iterations. Then we have the equation of a line (*t* parameterised on *i*).

The following table lists the predicted times²² for some selected sample models. The values for the total number of iterations, *i*, were known in advance.

| Model | <i>n</i> | <i>c</i> | <i>i</i> | <i>CSGMIN</i> | <i>TIMEND</i> | <i>t</i> | <i>t</i> * |
|----------|----------|----------|----------|---------------|---------------|----------|------------|
| HEATER | 168 | 1161 | 150 | 2677.961 | 8640 | 23 | 22 |
| EVAP2 | 99 | 153 | 9 | 2000 | 10000 | 1.3 | 1.5 |
| TESTCASE | 11 | 27 | 312 | 0.0165 | 2 | 1.9 | 2.1 |
| LBAR | 6 | 6 | 1520 | 3.4598 | 100 | 3.4 | 2.6 |
| TGMODAL | 58 | 91 | 1498 | 6.7592 | 2500 | 27 | 23 |
| TGTRAN | 58 | 91 | 1496 | 6.7592 | 2500 | 26 | 23 |

One can see that the predictions are still good for the transient-state solution routines.

As an example, the values for the number of iterations and *CSGMIN* are tabulated below for the *LBAR* example. The subroutine used is *SLFWBK* (Crank-Nicholson—implicit forward-backward differencing). The initial value for *CSGMIN* occurs at node 1 and is around 3.45982 seconds. Notice how it changes slightly as the simulation goes on; in a more realistic case the changes will be greater.

²² All of which (*CSGMIN*, *TIMEND*, *t*, *t**) are given in seconds.

| Simulation time | Iterations | CSGMIN | Simulation time | Iterations | CSGMIN |
|-------------------|------------|-------------------|-------------------|------------|-------------------|
| 3.286799907684326 | 18 | 3.459823738505052 | 55.87559843063354 | 100 | 3.459786378090168 |
| 6.573599815368652 | 17 | 3.459816189975047 | 59.16239833831787 | 16 | 3.459784873533585 |
| 9.860399723052979 | 100 | 3.459812237456282 | 62.44919824600220 | 15 | 3.459783369259751 |
| 13.14719963073730 | 19 | 3.459809259578331 | 65.73599815368652 | 100 | 3.459781863575965 |
| 16.43399953842163 | 18 | 3.459806757934513 | 69.02279806137085 | 16 | 3.459780355193491 |
| 19.72079944610596 | 18 | 3.459804549275543 | 72.30959796905518 | 100 | 3.459778843130432 |
| 23.00759935379028 | 17 | 3.459802540259411 | 75.59639787673950 | 17 | 3.459777326637939 |
| 26.29439926147461 | 19 | 3.459800674094908 | 78.88319778442383 | 16 | 3.459775805144148 |
| 29.58119916915894 | 18 | 3.459798912398994 | 82.16999769210815 | 16 | 3.459774278211593 |
| 32.86799907684326 | 17 | 3.459797227647376 | 85.45679759979248 | 100 | 3.459772745504870 |
| 36.15479898452759 | 100 | 3.459795599485074 | 88.74359750747681 | 100 | 3.459771206766071 |
| 39.44159889221191 | 18 | 3.459794012630688 | 92.03039741516113 | 15 | 3.459769661796132 |
| 42.72839879989624 | 100 | 3.459792455530702 | 95.31719732284546 | 100 | 3.459768110440671 |
| 46.01519870758057 | 100 | 3.459790919422188 | 98.60399723052979 | 17 | 3.459766552579233 |
| 49.30199861526489 | 100 | 3.459789397649417 | 101.8907971382141 | 13 | 3.459766552579233 |
| 52.58879852294922 | 100 | 3.459787885153972 | | | |

9.3.6 Is ESATAN able to perform a real-time simulation?

Let us consider the previous simplified transient state simulation scheme, that is, without outputs —just recomputing the nodal temperatures in each timestep. The CPU time required for a single timestep will be approximately $t_i \bar{I}$, being \bar{I} the "average" number of iterations employed in it²³. $t_i(n,c)$ is the time per iteration, as defined some pages before. Then, the quotient

$$\frac{t_i \times \bar{I}}{DTIMEU}$$

will give us the ratio between computer time and real time. The relation²⁴

²³ For many observed cases it is 1 iteration per timestep.

²⁴ The "less than" operators (\leq) should really mean "approximately less than" because of the simplifications introduced, but unhappily WordPerfect 5.2 —as many other things— lacks this symbol.

$$\frac{t_i \times \bar{I}}{DTIMEU} \leq 1 \quad \Leftrightarrow \quad t_i \times \bar{I} \leq DTIMEU$$

gives us the condition that ESATAN must satisfy in order to be "real time." It depends on n , c , \bar{I} , $DTIMEU$ and the processor speed, which is 8.4 MIPS for our analysis²⁵. The reader can verify that ESATAN runs in real time for all the former examples. For a bigger model with $n = 500$ nodes, $c = 3000$ conductors (typical for a satellite), $\bar{I} = 1$ iteration per timestep and timesteps of 1 second (= $DTIMEU$), it will still support real time (the real-time ratio is 44%), but for an even bigger model with $n = 800$, $c = 8000$ it will break down (real time ratio of 112%). In this case, a more powerful processor should be used to ensure a real-time simulation.

9.4 The SOHO Satellite Input Deck

The author was given the opportunity to test ESATAN with the SOHO²⁶ Satellite Thermal Input Deck (Phase C/D 2, Service Module - SVM). This input deck is representative of a "real world" thermal model. It has been prepared by the spanish company Construcciones Aeronáuticas, S. A. (CASA) for use at ESTEC with ESATAN.

The entire input deck is divided into the following files, which once preprocessed build up the final model:

- *I100.DAT*, *I200.DAT*, *I300.DAT*, *I400.DAT*: these files contain the sub-models *I1*, *I2*, *I3* and *I4* respectively, which in turn correspond to the +Y+Z, -Y+Z, -Y-Z, +Y-Z quarters of the internal enclosure of the satellite in a reference system in which the main platform lies on the YZ plane.
- *E5CS00.DAT*, *E5HS00.DAT*: contain the sub-model for the external enclosure for two test cases, cold (*E5C*) and hot (*E5H*), respectively. In the cold case the total disipation power is 1441 watts while in the hot case it is set to 1353 watts; the difference is due to different power values in the heaters as well as putting to work selected sets of them.
- *ST3400.DAT*: contains the main model, which consists of *I1*, *I2*, *I3*, *I4* and exactly one of *E5C* and *E5H* (plus the inter-model conductors and some few new nodes and conductors that are added in *ST3400.DAT*).

²⁵ One can take t_i (and, in general, the rest of the time values) as inversely proportional to the processor speed. Then, the former expression generalised for a computer with a speed of *MIPS* turns into

$$\frac{t_i \times \bar{I}}{DTIMEU} \times \frac{8.4}{MIPS} \leq 1$$

²⁶ The name SOHO stands for "Solar and Heliospheric Observatory." It should be launched by the ATLAS rocket in mid-1995 and it will be placed on a halo orbit around the first Lagrangian point of the Sun-Earth system, L_1 , which lies in the line Sun-Earth at 1.5 million kilometres from the Earth. Hence it never goes through the Earth shadow and it suffers no eclipses.

Basically, the **\$EXECUTION** block of this file first sets the initial state (temperatures, heat flows etc.); then computes the steady state for the cold case (that is, *E5C* is enabled and *E5H* disabled); beginning from this point, the steady state for the hot case is computed (with *E5C* disabled and *E5H* enabled). The ESATAN library routine used to calculate the steady state is *SOLVIT*.

The following table summarises the size of the SOHO thermal mathematical model:

| File name | File size (Kbytes) | Model name | Nodes (<i>n</i>) | Conductors (<i>c</i>) |
|------------|--------------------|------------|--------------------|-------------------------|
| I100.DAT | 105 | I1 | 64 | 1846 |
| I200.DAT | 72 | I2 | 45 | 1588 |
| I300.DAT | 66 | I3 | 43 | 876 |
| I400.DAT | 148 | I4 | 84 | 3033 |
| E5CS00.DAT | 297 | E5C | 390 | 5912 |
| E5HS00.DAT | 291 | E5H | 390 | 5589 |
| ST3400.DAT | 163 | ST34 | 14 | 1861 |
| | | Cold model | 640 | 14895 |
| | | Hot model | 640 | 14572 |

All the nodes are diffusion nodes (except for a dozen of boundary nodes). The conductors are either purely radiative (92% of the total) or purely conductive (8%).

Now some measures are given, as well as the predicted values using the models presented above²⁷.

The following table lists the **preprocessing** time for the submodels. One can see that the predictions of the formula tend to be quite greater than the measured ones.

²⁷ The models had been developed 6 months before.

| File name | File size (bytes) | Declarative size (bytes) | Preprocessing time (s) | Predicted time (s) |
|------------|-------------------|--------------------------|------------------------|--------------------|
| I100.DAT | 107391 | 71579 | 32.2 | 67.9 |
| I200.DAT | 73268 | 42475 | 21.6 | 46.0 |
| I300.DAT | 67588 | 35788 | 18.5 | 42.1 |
| I400.DAT | 151736 | 114052 | 58.5 | 96.7 |
| E5CS00.DAT | 304340 | 242697 | 138.3 | 194.0 |
| E5HS00.DAT | 298211 | 231755 | 126.4 | 188.0 |

The following table lists the **execution time for a steady state run** for both test cases separately, that is, beginning from the same initial state but one using the cold model and the other one the hot model, and calling the *SOLVIT* routine for the solution and *PRNDTB(' ', 'L,T', CURRENT)* for the output (that is, they are structurally analogue to the skeleton input deck proposed above). In both cases the number of iterations executed in the *SOLVIT* routine was 102.

| Model | Execution time (s) | Predicted time (s) |
|-------|---------------------------------------|--------------------|
| Cold | 169 (out of: 170, 180, 147, 198, 147) | 177 |
| Hot | 151 (out of: 139, 142, 142, 180, 156) | 174 |

The predicted values agree acceptably with the measured ones and are between the given maximum error bounds, although they tend to exceed the real ones, too. One should also notice that the variance is quite high, especially in the cold model. The time per iteration t_i is 1.66 s for the cold model and 1.48 s for the hot one, whilst the predicted ones are around 1.74 s and 1.72 s, respectively.

A **transient** was also prepared for the cold model. The input deck used is exactly the same as for the steady state but *SLFRWD* in one case and *SLFWBK* in the other one are called instead of *SOLVIT* and the control constants *OUTPUT* and *TIMEND* are set accordingly. The time per iteration t_i was 1.17 s whilst the predicted one is 1.69 s; the difference here is bigger compared with the steady state case.

For the transient case, the ratio real time/computer time was around 0.65 (26 minutes computer time for a transient of 1000 seconds real time)²⁸.

²⁸ So it did not run in real time. However the new server is, as mentioned, 2.6 times faster and the ratio grows to 1.7, achieving then real time.

In summary, the predictive models developed have a tendency to overestimate the time for big models (that is, they give a conservative estimate), but are still acceptable for our purposes.

9.5 ESATAN v5.5 vs ESATAN v6.3

In terms of performance, ESATAN v6.3 results to be around 5% faster in preprocessing and 15% faster in executing a simulation. This values are the outcome of a set of test runs carried out on both versions using the sample input decks provided with ESATAN v5.5.

LIST OF REFERENCES²⁹

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- SH-CAS-NT-00041: "SOHO—SVM: Heat Capacity Model Phase C/D2." CASA (División Espacio). 31/03/93.

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²⁹ The mentioned releases for the User's Manual, Engineering Manual and Training Manual are all compatible with ESATAN package version 5.

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APPENDIX A: Regression Fits

Given the set of data (y_i, \mathbf{x}_i) where $y_i \in \mathbb{R}$, $\mathbf{x}_i \in \mathbb{R}^m$, for $i = 1, \dots, n$, a least-squares regression fit of y as a function of $\mathbf{x} = (x_1, \dots, x_n)$ and with parameters $\mathbf{p} = (p_1, \dots, p_l)$ can be expressed as:

$$y^*(\mathbf{x}, \mathbf{p})$$

$$\min_{\mathbf{p} \in \mathbb{R}^l} \overline{E^2}(\mathbf{p}) = \min_{\mathbf{p}} \left\{ \frac{1}{n} \sum_{i=1}^n (y_i - y_i^*)^2 \right\} = \min_{\mathbf{p}} \left\{ \frac{1}{n} \sum_{i=1}^n (y_i - y^*(\mathbf{x}_i, \mathbf{p}))^2 \right\}$$

Under some conditions one can take partial derivatives of E^2 with respect to each parameter, set them equal to 0 and solve the resulting system of l equations with l unknowns p_1, \dots, p_l ³⁰:

$$\frac{\partial \overline{E^2}}{\partial p_j} = 0, \quad j = 1, \dots, l$$

Some particular fits of use for this report are given below, along with the system whose solution gives the optimum values for the parameters:

● Linear bidimensional fit: $y^*(x_1, x_2; A, B, C) = Ax_1 + Bx_2 + C$. The optimum values of A , B and C satisfy the system

$$\begin{pmatrix} 20 & 11 & 10 \\ 11 & 02 & 01 \\ 10 & 01 & 00 \end{pmatrix} \begin{pmatrix} A \\ B \\ C \end{pmatrix} = \begin{pmatrix} \overline{x_1 y} \\ \overline{x_2 y} \\ \overline{y} \end{pmatrix}$$

● Linear unidimensional fit: $y^*(x; A, B) = Ax + B$.

³⁰ Another approach to solve the regression fit is to optimise the objective function

$$f(\mathbf{p}) = \frac{1}{n} \sum_{i=1}^n (y_i - y^*(\mathbf{x}_i, \mathbf{p}))^2$$

in the p -space. A variety of algorithms for unconstrained multiparameter optimisation (non-linear programming) exists, such as the Hooke & Jeeves method, PARTAN etc. Many of them can use a Fibonacci search to minimise the number of function evaluations, which proves to be very valuable in our case, as computing $t(n, c, i)$ means editing the input deck (to set the values for *RELXCA* and *NLOOP*), preprocessing it, running the executable file four or five times (to get a reliable average) and inspecting the corresponding LOG files to find out the elapsed CPU time.

$$\begin{pmatrix} 2 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} A \\ B \end{pmatrix} = \begin{pmatrix} \overline{xy} \\ \overline{y} \end{pmatrix}$$

- Quadratic unidimensional fit: $y^*(x; A, B, C) = Ax^2 + Bx + C$.

$$\begin{pmatrix} 4 & 3 & 2 \\ 3 & 2 & 1 \\ 2 & 1 & 0 \end{pmatrix} \begin{pmatrix} A \\ B \\ C \end{pmatrix} = \begin{pmatrix} \overline{x^2y} \\ \overline{xy} \\ \overline{y} \end{pmatrix}$$

- $y^*(x_1, x_2; A, B, C, D) = Ax_2 + Bx_1^2 + Cx_1 + D$.

$$\begin{pmatrix} 02 & 21 & 11 & 01 \\ 21 & 40 & 30 & 20 \\ 11 & 30 & 20 & 10 \\ 01 & 20 & 10 & 00 \end{pmatrix} \begin{pmatrix} A \\ B \\ C \\ D \end{pmatrix} = \begin{pmatrix} \overline{x_2y} \\ \overline{x_1^2y} \\ \overline{x_1y} \\ \overline{y} \end{pmatrix}$$

✎ We use the following compact notation for the arithmetical mean of a cross-product (in a 2D space): for $\alpha, \beta \in \{1, 2\}$, $\alpha \neq \beta$, $a, b \in \mathbb{N} \cup \{0\}$,

$$\overline{x_\alpha^a x_\beta^b} \triangleq \frac{1}{n} \sum_{i=1}^n x_{\alpha i}^a x_{\beta i}^b \triangleq ab$$

For example

$$\overline{x_1^2 x_2} \triangleq \frac{1}{n} \sum_{i=1}^n x_{1i}^2 x_{2i} \triangleq 21$$

The error indicators we use are:

$$\text{Mean relative error: } \bar{\epsilon} \triangleq \frac{1}{n} \sum_{i=1}^n \left| \frac{y_i - y_i^*}{y_i} \right|$$

$$\text{Maximum relative error: } \epsilon_{\max} \triangleq \max_{i=1, \dots, n} \left\{ \left| \frac{y_i - y_i^*}{y_i} \right| \right\}$$

Be aware that they are just indicators. If we say that the maximum relative error

equals k , we are saying that for all the points measured, the relative error calculated a posteriori will not exceed k . But one has to take into account that it is not the same a relative error of 15% in a running time of 120 hundredths of second (where 18 hundredths of second are hidden by the background noise) as in 30 seconds (where 4.5 seconds make a difference).

Furthermore, those indicators are not the minimisation criterion used in the least-squares method.

APPENDIX B: Experimental Data

Table II.1: (s_i, d_i, t_i) where $t(s, d)$ is the preprocessing time of an input deck with s bytes, d of which belong to definition sentences.

The final value for $t(s, d)$ was calculated as the average of several different runs of the preprocessor on the same input deck.

| Model | s | d | t | t^* |
|----------|-------|-------|------|-------|
| FLOWPIPE | 2392 | 1340 | 6.5 | 5.79 |
| HEATER | 48827 | 42847 | 31.0 | 35.97 |
| MATRIX | 11320 | 1997 | 9.6 | 9.81 |
| NLBAR | 7293 | 1050 | 6.9 | 7.84 |
| SAVEXX | 26572 | 21950 | 31.0 | 21.26 |
| STEADY | 2053 | 295 | 3.5 | 5.39 |
| TESTCASE | 3773 | 1013 | 4.6 | 6.31 |
| TGMODAL | 3898 | 2593 | 8.0 | 6.75 |
| TGTRAN | 12057 | 2652 | 10.2 | 10.28 |
| LBAR | 1028 | 475 | 3.1 | 4.99 |

Table II.2: for each model available the running time t is given for different combinations of n , c and i (no. of nodes, conductors and iterations, respectively).

All the values for t , t_i and t_o are in hundredths of second.

The values of *NLBAR* were discarded for the fit of t_i as they are clear outliers and the same happened to the values of c different from 1161 of *HEATER* for the fit of t_o .

| Model name | <i>n</i> | <i>c</i> | (<i>i,t</i>) | <i>t_i</i> | <i>t_o</i> |
|------------|----------|----------|--|----------------------|----------------------|
| HEATER | 168 | 1161 | (10,273) (50,890) (100,1494) (150,2260) (200,2959) | 14.0 | 143 |
| | | 700 | (10,214) (50,630) (100,1108) (150,1646) (200,2148) | 10.2 | 111 |
| | | 337 | (10,181) (50,416) (100,714) (150,1054) (200,1351) | 6.2 | 110 |
| | | 100 | (10,151) (50,278) (100,444) (150,638) (200,814) | 3.52 | 106 |
| SAVEXX | 208 | 615 | (3,210) (54,690) (135,1478) (285,2972) | 9.81 | 167 |
| | | 407 | (3,188) (54,538) (135,1169) (285,2211) | 7.21 | 167 |
| | | 305 | (3,161) (54,493) (135,982) (285,1960) | 6.36 | 140 |
| | | 140 | (3,160) (54,376) (135,749) (285,1435) | 4.54 | 139 |
| FLOWPIPE | 26 | 51 | (10,105) (50,136) (75,154) (100,168) | 0.709 | 99.3 |
| | | 43 | (10,105) (50,130) (75,145) (100,160) | 0.621 | 98.6 |
| | | 31 | (10,104) (50,123) (75,139) (100,151) | 0.531 | 97.7 |
| | | 19 | (10,102) (50,119) (75,133) (100,144) | 0.475 | 96.4 |
| STEADY | 6 | 8 | (10,101) (50,112) (250,122) (1250,231) (6250,821) | 0.115 | 97 |
| LBAR | 6 | 6 | (10,91) (100,97) (252,117) (1000,216) (5000,719) | 0.126 | 87.1 |
| NLBAR | 6 | 11 | (10,92) (30,89) (50,97) (100,122) (150,128) (200,150) (250,156) (408,196) | 0.275 | 87.5 |
| TESTCASE | 11 | 27 | (100,125) (1000,460) (3000,1150) (5000,1890) | 0.358 | 91.2 |
| | | 20 | (100,122) (1000,413) (3000,1027) (5000,1590) | 0.3 | 107 |
| | | 14 | (100,118) (1000,375) (3000,930) (5000,1400) | 0.262 | 109 |
| TGMODAL | 58 | 91 | (5,118) (25,159) (100,253) (125,313) (200,448) (307,536) | 1.43 | 124 |
| | | 65 | (5,118) (25,130) (100,223) (125,260) (200,350) (307,466) | 1.18 | 108 |
| | | 53 | (5,116) (25,134) (100,210) (125,240) (200,332) (307,438) | 1.08 | 107 |
| | | 30 | (5,107) (25,135) (100,194) (125,209) (200,294) (307,380) | 0.9 | 106 |
| TGTRAN | 58 | 91 | (5,108) (25,132) (100,270) (125,275) (200,363) (307,512) | 1.32 | 109 |
| EVAP2 | 99 | 153 | (1,115) (10,137) (30,193) (50,232) | 2.43 | 114 |
| MATRIX | 8 | 7 | (3,93) (100,109) (500,181) (1000,248) (5000,846) | 0.15 | 97.5 |

APPENDIX C: Fit Formulae for the Performance Evaluation

Preprocessing time

Being s the size in bytes of the input deck and d the size in bytes of its declarative part, the preprocessing time t in seconds for it can be approximated with a mean relative error of 25% and a maximum relative error of 60% as

$$t^*(s, d) = As + Bd + C$$

$$A = 4.3 \cdot 10^{-4} \text{ s/byte} \quad B = 2.4 \cdot 10^{-4} \text{ s/byte} \quad C = 4.43 \text{ s}$$

Running time for our skeleton input deck

For an ESATAN skeleton input deck, let n be the number of nodes, c the number of conductors and i the number of iterations required. Then its running time in seconds can be approximated with a mean relative error of 5% and a maximum relative error of 16% as

$$t(n, c, i) = (\alpha c + \beta n^2 + \gamma n + \delta) i + \epsilon n + \zeta c + \eta$$

where $\alpha = 10^{-4}$, $\beta = 4 \cdot 10^{-7}$, $\gamma = 7.5 \cdot 10^{-5}$, $\delta = 0$, $\epsilon = 2.6 \cdot 10^{-3}$, $\zeta = 1.2 \cdot 10^{-4}$, $\eta = 0.93$ (all the parameters are in seconds).

Real-time capability for a simplified transient state simulation scheme

Being t_i the CPU time per iteration, n the number of nodes, c the number of conductors, \bar{I} the average number of iterations per timestep, $DTIMEU$ the length in seconds of the timestep and $MIPS$ the speed processor in MIPS, the relation

$$\frac{t_i(n, c) \times \bar{I}}{DTIMEU} \times \frac{8.4}{MIPS} \leq 1$$

should be satisfied with *some* slack for real time to be achieved.