

# Progressive & Algorithms & Systems

**Florin Rusu**

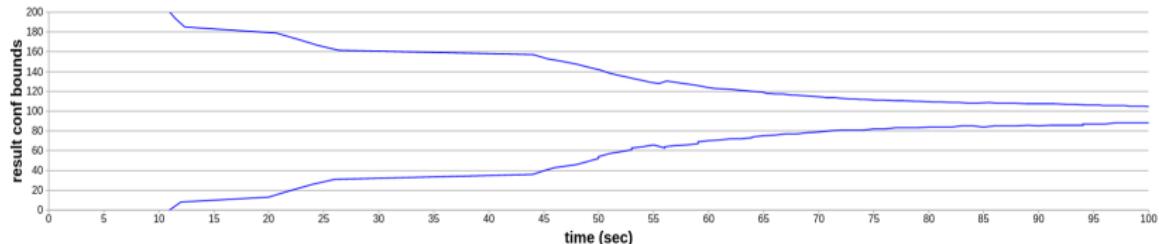
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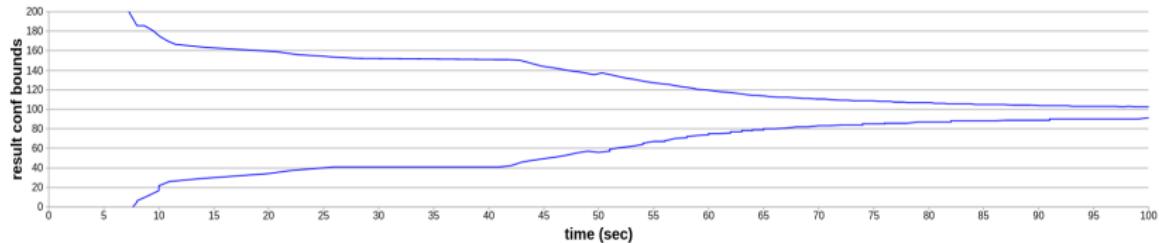


# Progressive Computation for Data Exploration

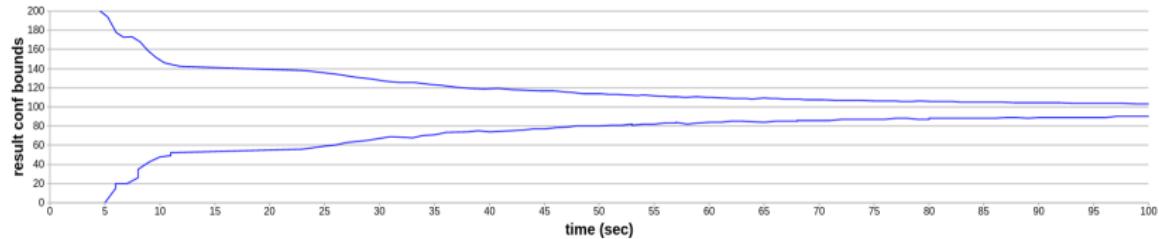
```
>>> select count(*) from candidates where mag > 10
```



```
>>> select count(*) from candidates where mag > 10 and mag < 100
```

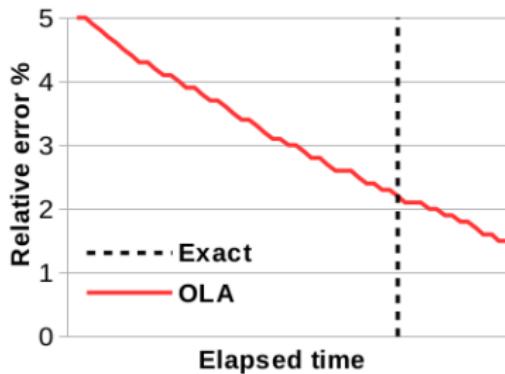
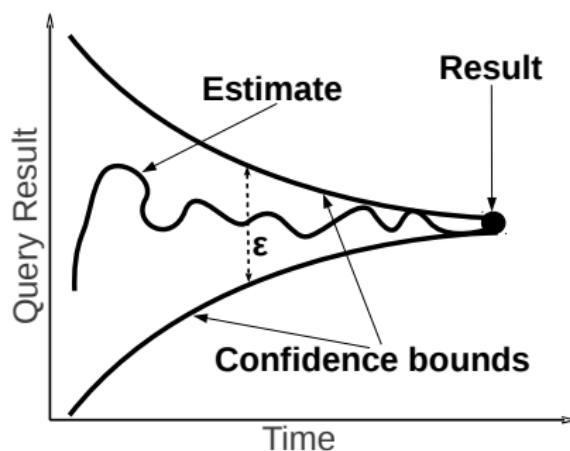


```
>>> select count(*) from candidates where mag > 10 and mag < 200
```



# Progressive Computation

## Online Aggregation (OLA) in DB

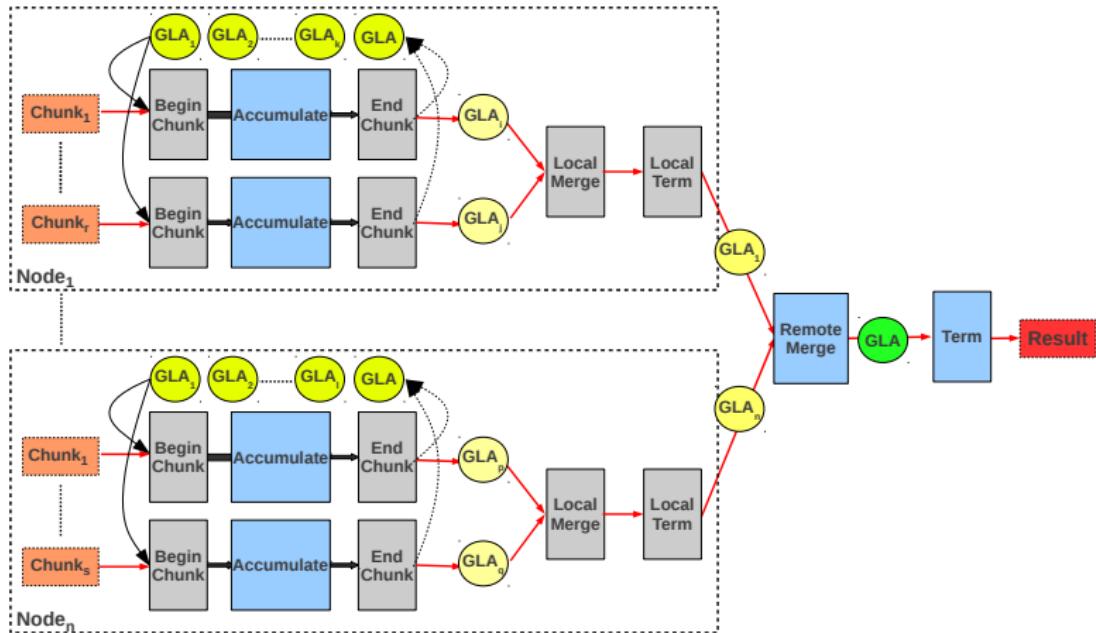


- How to derive confidence bounds that shrink progressively?
- How to generate a meaningful estimate and confidence bounds as early as possible?
- How to minimize the estimation overhead?

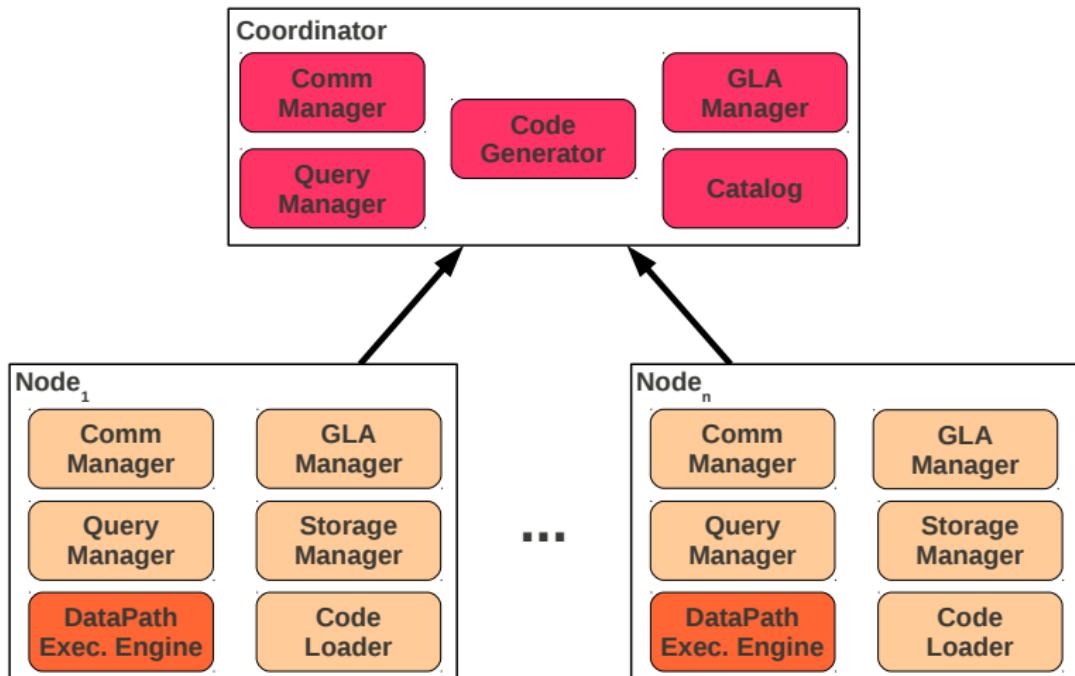
1 PF-OLA: Parallel Framework for Online Aggregation

2 OLA-GD: Online Aggregation for Gradient Descent Optimization

3 OLA-RAW: Online Aggregation over Raw Data

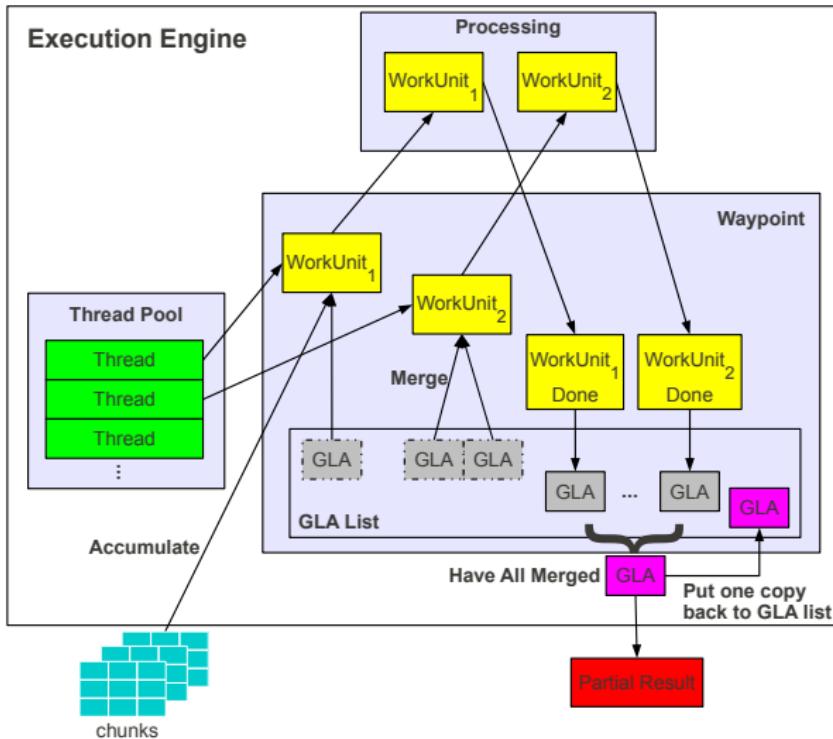


# GLADE Architecture



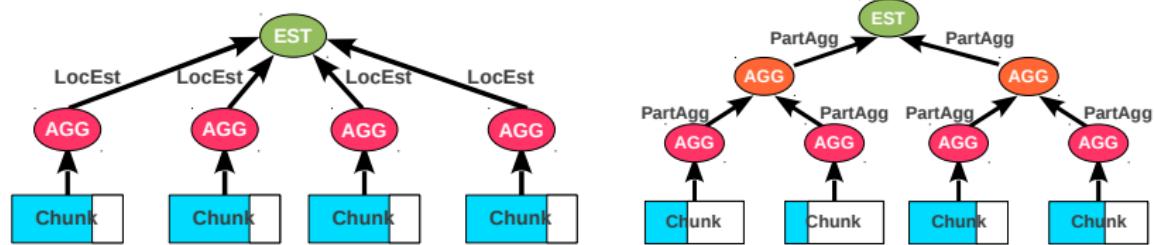
Method	Usage
Init () Accumulate (Item $d$ ) Merge (UDA $input_1$ , UDA $input_2$ , UDA $output$ ) – local and remote Terminate () – local and final	Basic interface
BeginChunk() EndChunk ()	Chunk processing
Serialize () Deserialize ()	Transfer UDA across processes
EstimatorTerminate () EstimatorMerge (UDA $input_1$ , UDA $input_2$ , UDA $output$ )	Progressive computation
Estimate ( <i>estimator</i> , <i>lower</i> , <i>upper</i> , <i>confidence</i> )	OLA estimation

# Partial Aggregation



- Centralized random shuffling
  - Permute data randomly at loading
  - Scan produces larger samples
- Stratified sampling
  - Permute data randomly in each partition
  - Direct extension of random shuffling to partitioned data
- Global data randomization at loading
  - Split data randomly at each node
  - Permute all received data randomly
  - Standard hash-based data partitioning

# Sample Aggregation



- Centralized
- Distributed tree

# Generic Sampling Estimator

```
AGG ←= SELECT SUM(f(d))  
        FROM D  
        WHERE P(d)
```

- $S$  is simple random sample without replacement from  $D$
- Estimator  $X = \frac{|D|}{|S|} \sum_{s \in S, P(s)} f(s)$

$$E[X] = \text{AGG}$$

$$\text{Var}[X] = \frac{|D| - |S|}{(|D| - 1)|S|} \left[ |D| \sum_{d \in D, P(d)} f^2(d) - \left( \sum_{d \in D, P(d)} f(d) \right)^2 \right]$$

$$\text{Est}_{\text{Var}[X]} = \frac{|D|(|D| - |S|)}{|S|^2(|S| - 1)} \left[ |S| \sum_{s \in S, P(s)} f^2(s) - \left( \sum_{s \in S, P(s)} f(s) \right)^2 \right]$$

- Data are partitioned across  $N$  nodes:  $D = D_1 \cup D_2 \cup \dots \cup D_N$
- Take samples  $S_i$ ,  $1 \leq i \leq N$  independently at each node

## Single Estimator

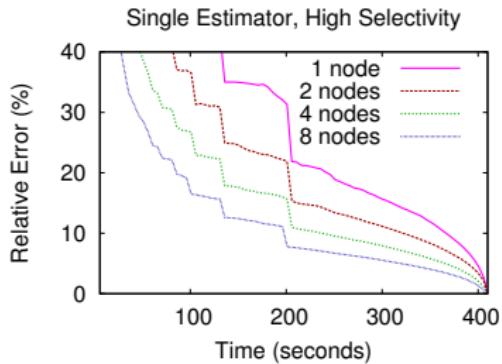
- Guarantee  
 $S = S_1 \cup S_2 \cup \dots \cup S_N$  is a sample from  $D$
- Synchronized estimator
  - $\frac{S_i}{D_i} = k$  (const),  
 $1 \leq i \leq N$
- Asynchronous estimator
  - Global data randomization

## Multiple Estimators

- Stratified sampling
- Build an estimator  $X_i$  for each partition  $D_i$ ,  
 $1 \leq i \leq N$ :  
$$X_i = \frac{|D_i|}{|S_i|} \sum_{s \in S_i, P(s)} f(s)$$
- $X = \sum_{i=1}^N X_i$  is unbiased
- $\text{Var} \left[ \sum_{i=1}^N X_i \right] = \sum_{i=1}^N \text{Var}[X_i]$

# Time to Convergence

```
SELECT n_name, SUM(l_extendedprice*(1-l_discount)*(1+l_tax))
FROM lineitem, supplier, nation
WHERE l_shipdate = 1993-02-26 AND l_quantity = 1 AND
l_discount between [0.02,0.03] AND
l_suppkey = s_suppkey AND s_nationkey = n_nationkey
GROUP BY n_name
```



- TPC-H scale **8,000 (8TB)**
- Single node: 16 cores @ 2GHz; 16GB RAM; 4 disks @ 110MB/s throughput/disk
- Cluster: 8 X worker + coordinator (9 nodes); Gigabit Ethernet; same rack

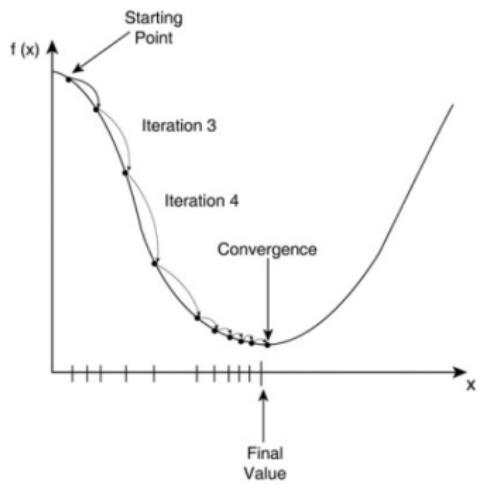
# Estimation Overhead

Query	Execution Time (seconds)	
	No estimation	OLA
Aggregate	222	222
Group <sub>small</sub>	344	345
Group <sub>large</sub>	404	407
Join	409	411

- Chengjie Qin and Florin Rusu. *Sampling Estimators for Parallel Online Aggregation*. BNCOD 2013, pp. 204–217.
- Chengjie Qin and Florin Rusu. *Parallel Online Aggregation in Action*. SSDBM 2013, pp. 383–386. [Demo]
- Chengjie Qin and Florin Rusu. *PF-OLA: A High-Performance Framework for Parallel Online Aggregation*. Distributed and Parallel Databases (DAPD), August 2013.

- 1 PF-OLA: Parallel Framework for Online Aggregation
- 2 OLA-GD: Online Aggregation for Gradient Descent Optimization
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# Gradient Descent Optimization



$$\min_{\vec{w} \in \mathbb{R}^d} \left\{ \Lambda(\vec{w}) = \sum_{(\vec{x}_i, y_i) \in \text{data}} f(\vec{w}, \vec{x}_i; y_i) \right\}$$

$$\vec{w}^{(k+1)} = \vec{w}^{(k)} - \alpha^{(k)} \nabla \Lambda \left( \vec{w}^{(k)} \right)$$

$\Lambda(\vec{w})$  is the loss

$\nabla \Lambda(\vec{w}) = \left[ \frac{\partial \Lambda(\vec{w})}{\partial w_1}, \dots, \frac{\partial \Lambda(\vec{w})}{\partial w_d} \right]$  is the gradient

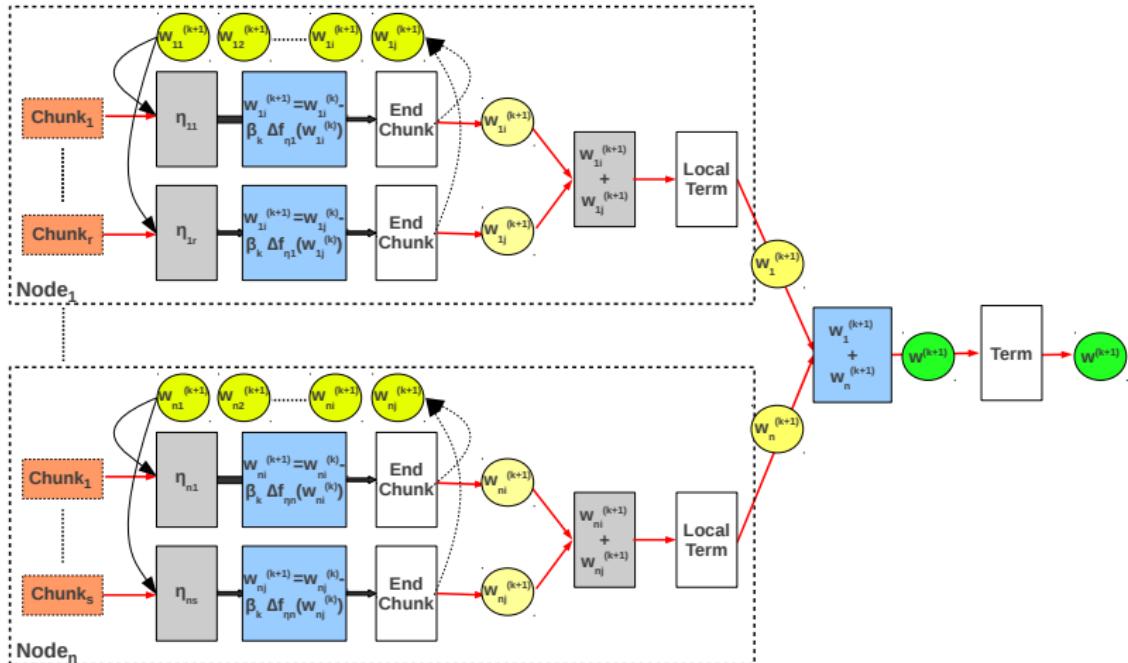
$\alpha^{(k)}$  is step size or learning rate

$\vec{w}^{(0)}$  is the starting point (random)

[http://www.yalidex.com/game-development/1592730043\\_ch18lev1sec4.html](http://www.yalidex.com/game-development/1592730043_ch18lev1sec4.html)

- Convergence to minimum guaranteed for convex objective function

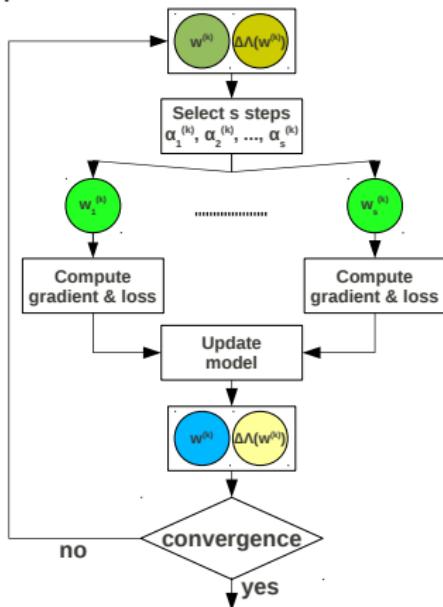
# Gradient Descent as GLADE GLA



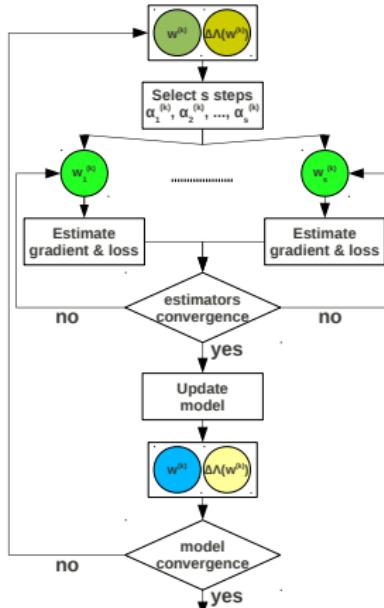
# Approximate Gradient Descent

Main idea: apply online aggregation (OLA) sampling to speed-up the execution of a speculative iteration

Speculative Gradient Descent



Approximate Gradient Descent



```

1: for each example  $(\vec{x}_{\eta(j)}, y_{\eta(j)})$  do
2:   for each active model  $\vec{w}_i$  do in parallel
3:     Estimate gradient  $G_i[\text{est}, \text{std}]$ :  $\nabla \Lambda(\vec{w}_i) \{(\vec{x}_{\eta(j)}, y_{\eta(j)})\}$ 
4:     Estimate loss  $L_i[\text{est}, \text{std}]$ :  $\Lambda(\vec{w}_i, \vec{x}_{\eta(j)}; y_{\eta(j)})$ 
5:   end for
6:   if estimators.convergence_check( $j$ ) then
7:     Prune out models:  $\text{Stop Loss}(\{L_i[\text{est}, \text{std}]\}_{i \leq s}, \epsilon_1)$ 
8:     Let  $t$  be the number of remaining models, i.e., active
9:     if  $\text{Stop Gradient}(\{G_{tl}[\text{est}, \text{std}]\}_{l \leq d}, \epsilon_2)$  then break
10:    Let  $s = t$ 
11:   end if
12: end for

```

## OLA sampling

- no pre-determined sample size
- avoid correlation between estimators by random data shuffling (at runtime)
- continuous sampling at runtime until estimators converge

```

SELECT
  ... , SUM( $f_q$ ) , ...
FROM data AS D
SELECT
  ... ,  $Z_q = \text{SUM}(f_q)$  , ...
  ... ,  $Z_q^2 = \text{SUM}(f_q^2)$  , ...
FROM sample AS S

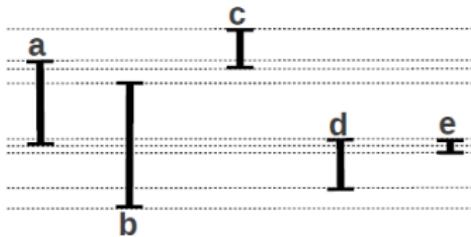
```

- estimator:  $Z_q \cdot \frac{|D|}{|S|}$
- variance:  $\frac{|D|(|D|-|S|)}{|S|^2(|S|-1)} \left( |S|Z_q^2 - (Z_q)^2 \right)$

# Approximate BGD

```
1: for each example  $(\vec{x}_{\eta^{(j)}}, y_{\eta^{(j)}})$  do
2:   for each active model  $\vec{w}_i$  do in parallel
3:     Estimate gradient  $G_i[\text{est}, \text{std}]$ :  $\nabla \Lambda(\vec{w}_i) \{ (\vec{x}_{\eta^{(j)}}, y_{\eta^{(j)})}) \}$ 
4:     Estimate loss  $L_i[\text{est}, \text{std}]$ :  $\Lambda(\vec{w}_i, \vec{x}_{\eta^{(j)}}, y_{\eta^{(j)}})$ 
5:   end for
6:   if estimators_convergence_check( $j$ ) then
7:     Prune out models: Stop Loss( $\{L_i[\text{est}, \text{std}]\}_{i \leq s}, \varepsilon_1$ )
8:     Let  $t$  be the number of remaining models, i.e., active
9:     if Stop Gradient( $\{G_{tl}[\text{est}, \text{std}]\}_{l \leq d}, \varepsilon_2$ ) then break
10:    Let  $s = t$ 
11:  end if
12: end for
```

- Identify step size with minimum loss based on estimate & confidence bounds
- Interacting estimators
- Exact pruning
- Approximate pruning

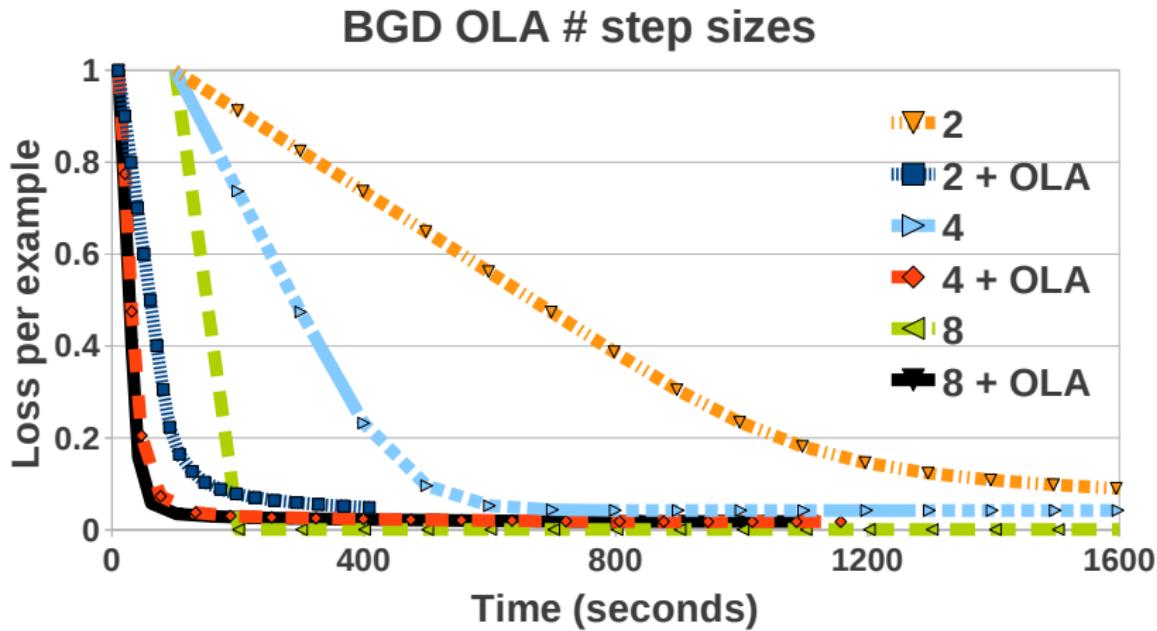


```
1: for each example  $(\vec{x}_{\eta^{(j)}}, y_{\eta^{(j)}})$  do
2:   for each active model  $\vec{w}_i$  do in parallel
3:     Estimate gradient  $G_i[\text{est}, \text{std}]$ :  $\nabla \Lambda(\vec{w}_i) \{(\vec{x}_{\eta^{(j)}}, y_{\eta^{(j)})}\}$ 
4:     Estimate loss  $L_i[\text{est}, \text{std}]$ :  $\Lambda(\vec{w}_i, \vec{x}_{\eta^{(j)}}; y_{\eta^{(j)}})$ 
5:   end for
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10:    Let  $s = t$ 
11:  end if
12: end for
```

- One estimator for each dimension in model  $\vec{w}$
- Grouped estimators

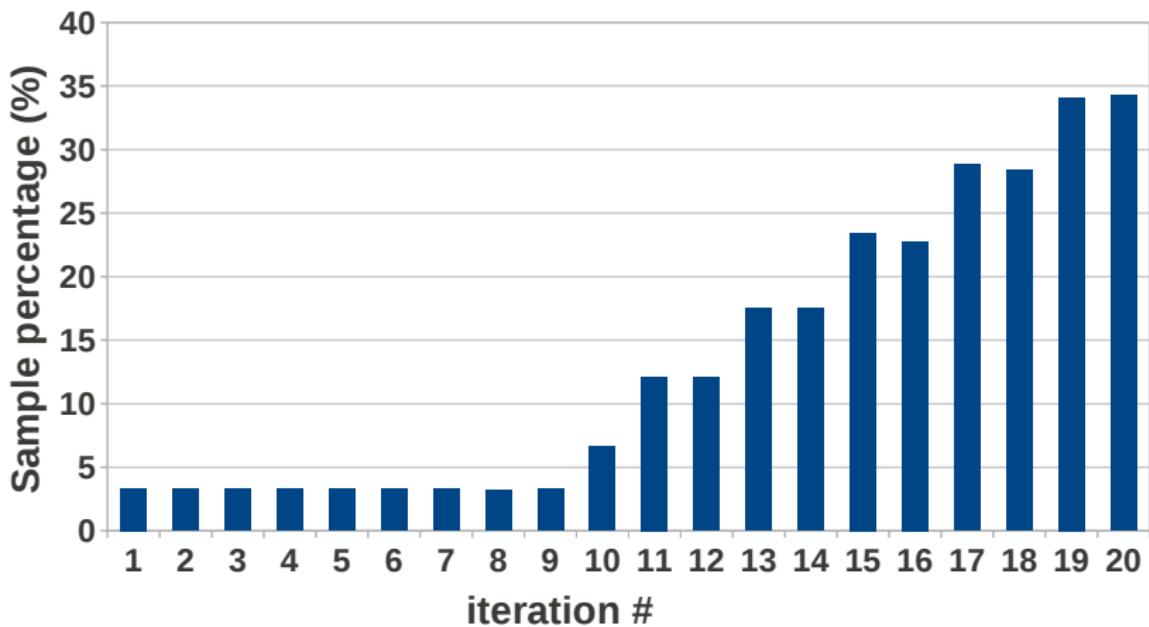
## When to stop?

- all estimators converge (million dimensions)
- percentage of estimators converge, e.g., 90%
- unified convergence threshold, e.g.,  $\varepsilon' = d \cdot \varepsilon$



- 50M examples, 200 dimensions, 136GB

# Sample Percentage

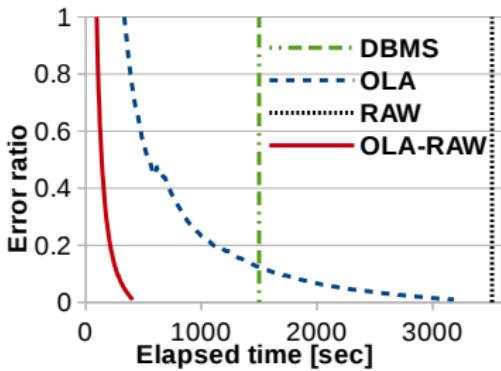
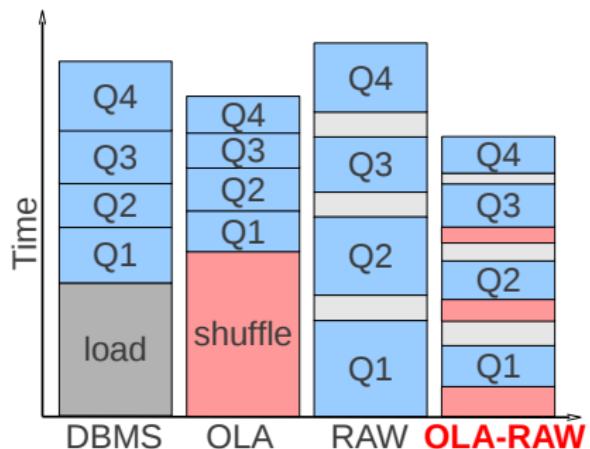


- 50M examples, 200 dimensions, 136GB

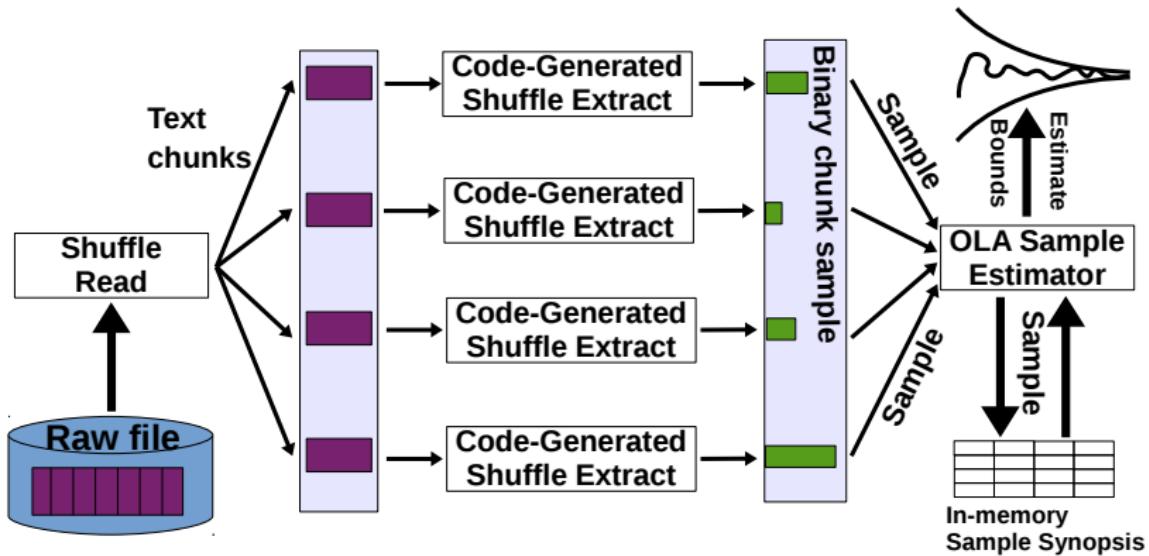
- Chengjie Qin and Florin Rusu. *Speculative Approximations for Terascale Analytics*. CoRR abs/1501.00255, December 2014.
- Chengjie Qin and Florin Rusu. *Speculative Approximations for Terascale Distributed Gradient Descent Optimization*. DanaC@SIGMOD 2015.
- Florin Rusu, Chengjie Qin, and Martin Torres. *Scalable Analytics Model Calibration with Online Aggregation*. IEEE Data Engineering Bulletin, Vol. 38, No. 3, pp. 30–44, September 2015.

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# Motivation & Approach



# OLA-Raw Architecture

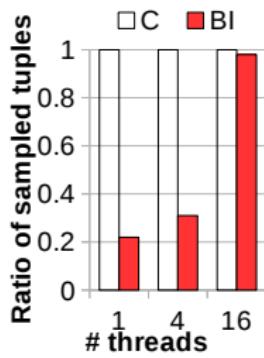
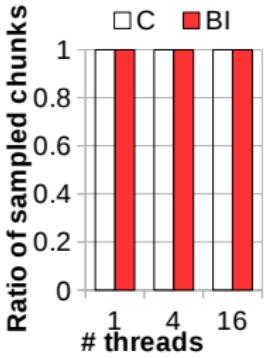
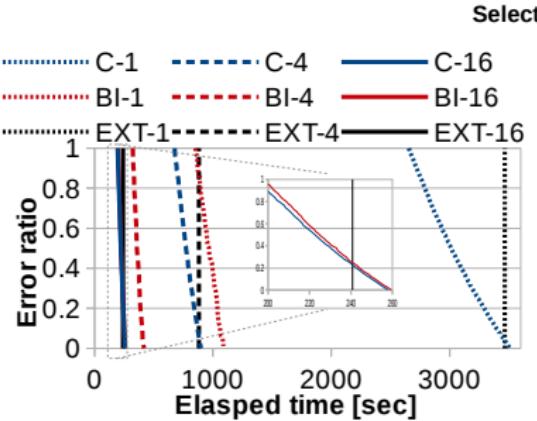
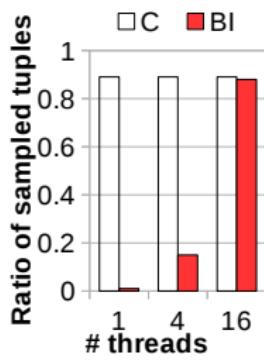
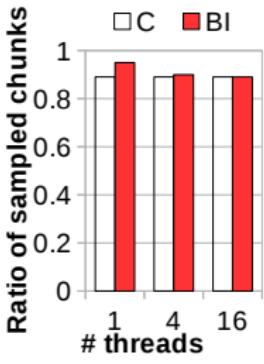
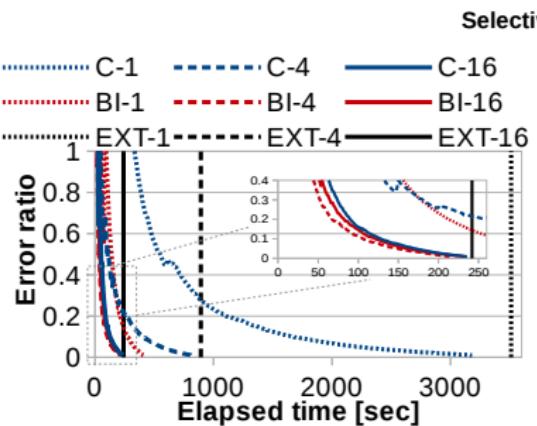


# Parallel Bi-Level Sampling

A	B				
4	0.8	1	14	3.75	Exact computation
242	0.427		562	21.23	2 1 4 2.5 6 2 5 1.2
36	0.6		3216	42.836	4521 90.837 8425 0.526 3439 10.332 7294 9.236
5724	1.236		72	0.1	4 0.8 242 0.427 36 0.6 5724 1.236
4521	90.837	4			1
8425	0.526	3			
3439	10.332	2			
7294	9.236	1			
2	1	4	14	3.75	Chunk-level sampling
4	2.5	4	562	21.23	2 1 4 2.5 6 2 5 1.2
6	2	4	3216	42.836	4521 90.837 8425 0.526 3439 10.332 7294 9.236
5	1.2	4	72	0.1	4 0.8 242 0.427 36 0.6 5724 1.236
14	3.75	3			1
562	21.23	4			3
3216	42.836	4	5724	1.236	2
72	0.1	1	7294	9.236	1
T		4			2

- Inspection paradox: result order  $\neq$  random chunk order

# Experimental Results



- Yu Cheng, Weijie Zhao, and Florin Rusu. *OLA-RAW: Scalable Exploration over Raw Data*. CoRR abs/1702.00358, February 2017.
- Yu Cheng, Weijie Zhao, and Florin Rusu. *Bi-Level Online Aggregation on Raw Data*. SSDBM 2017.

# Thank you!

# Questions?